

# Implications of lepton number violation on high-scale baryogenesis and dark matter

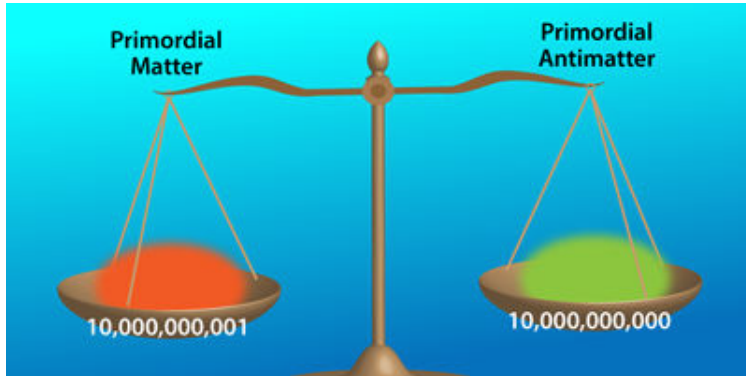
CP<sup>3</sup> Origins  
Wei-Chih Huang  
03.01.2018  
IOP Academia Sinica

F. Deppisch, J. Harz, WCH, M. Hirsch, H. Päs, Phys. Rev. D92 (2015) 036005  
F. Deppisch, L. Graf, J. Harz, WCH, arXiv:1711.10432  
M. T. Frandsen, C. Hagedorn, WCH, E. Molinaro, H. Päs, arXiv:1801.XXXXX

# Outline

- Motivations
- Sakharov Conditions
- Introduction on mechanisms for baryon asymmetry generation
- L-violation responsible for  $0\nu\beta\beta$  decay and wash-out on L and B
- Tree- and loop-level contributions to  $0\nu\beta\beta$  decay
- Connection to asymmetric dark matter (ADM)
- Conclusions

# Motivation



# Sakharov Conditions

- B violation
- C and CP violation:

$$X \rightarrow B$$

$$\overline{X} \rightarrow \overline{B}$$

➔ Total baryon number is still conserved if C or CP is conserved.

# Sakharov Conditions

- C and CP violation:

$$iM_1(X \rightarrow B + Y) = a$$

$$iM_2(X \rightarrow B + Y) = B \times C e^{i\theta}$$

$$i\bar{M}_1(\bar{X} \rightarrow \bar{B} + \bar{Y}) = a^*$$

$$i\bar{M}_2(\bar{X} \rightarrow \bar{B} + \bar{Y}) = B^* \times C e^{i\theta}$$

$$\Gamma(X \rightarrow B + Y) - \Gamma(\bar{X} \rightarrow \bar{B} + \bar{Y}) = 4 \int d\Pi_f |AB^*| \sin \phi_{AB} \sin \theta$$

$$AB^* = |AB^*| e^{i\phi_{AB}}$$

# Sakharov Conditions

- Out of equilibrium dynamics since in thermal equilibrium, we have  $\langle B \rangle = 0$

Baryon number  $B$  is odd under  $C$ , even under  $P$  and  $T$   
 $\Rightarrow B$  is odd under  $CPT \equiv \theta$

$$\begin{aligned}
 \langle B \rangle_T &= \text{Tr} \left( e^{-H/T} B \right) \\
 &= \text{Tr} \left( \theta^{-1} \theta e^{-H/T} B \right) \\
 &= \text{Tr} \left( e^{-H/T} \theta B \theta^{-1} \right) \\
 &= -\langle B \rangle_T
 \end{aligned}$$

# Sphalerons

- Sphaleron processes (Klinkhammer & Manton '84; Kuzmin et al. '85) convert lepton asymmetry into baryon asymmetry

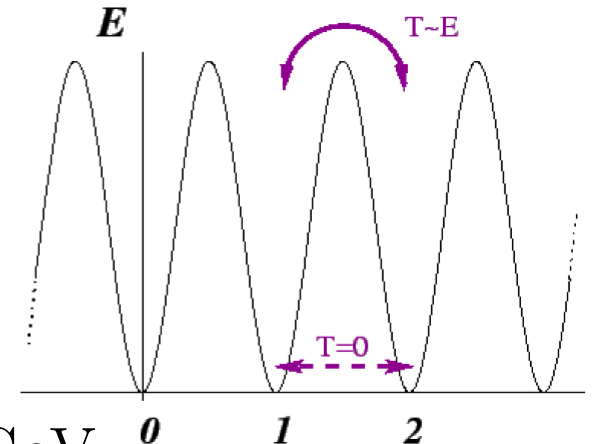
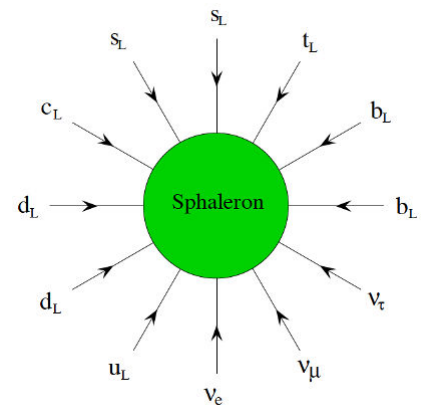
$$j_5^\mu = \bar{\psi} \gamma_5 \gamma^\mu \psi, \quad \partial_\mu j_5^\mu = \frac{1}{16\pi^2} \tilde{F}_{\mu\nu} F^{\mu\nu} = \frac{\epsilon_{\rho\sigma\mu\nu}}{16\pi^2} F^{\rho\sigma} F^{\mu\nu} .$$

$$\Delta Q^i = \frac{1}{64\pi^2} \int d^4x F_{\mu\nu}^A \tilde{F}^{\mu\nu A} \quad \text{Winding or Chern-Simons number of the field configuration}$$

$$\Delta B = \Delta L = 3$$

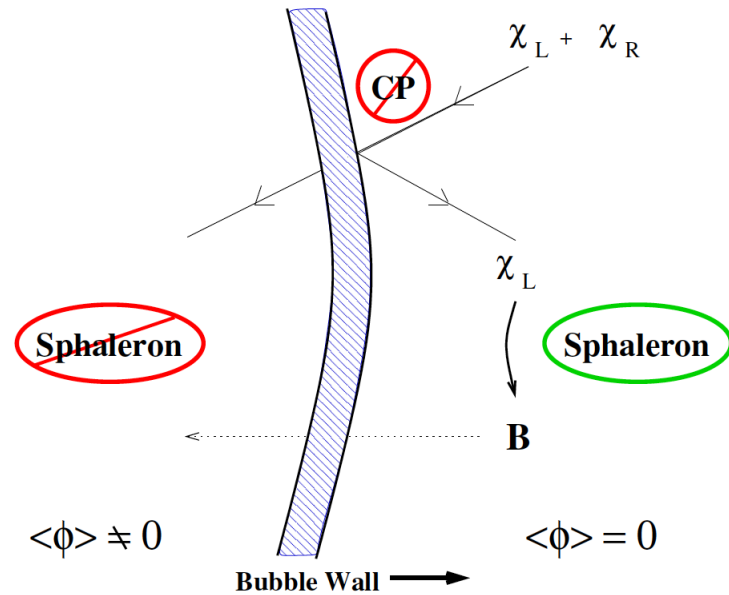
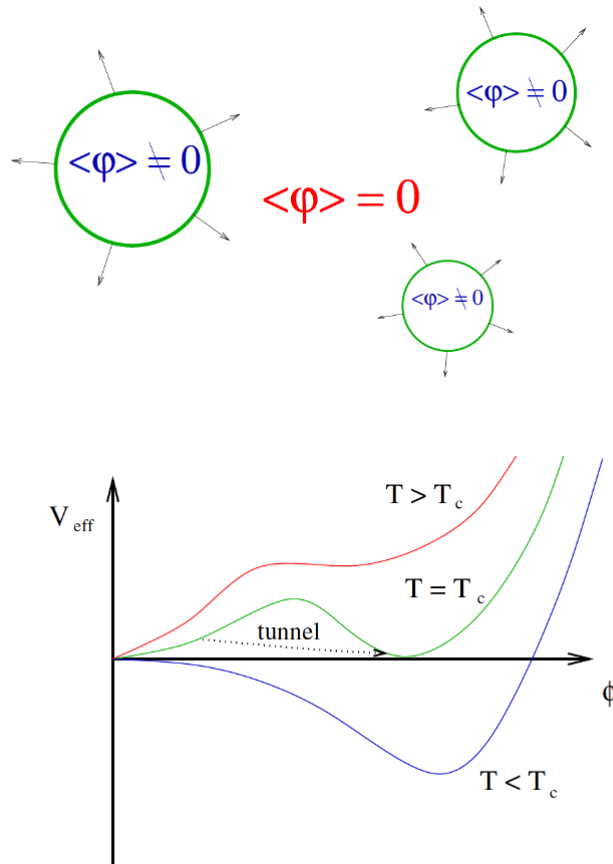
$$\mathcal{O}_{B+L} = \prod_{i=1,2,3} (q_{L_i}, q_{L_i}, q_{L_i} \ell_{L_i})$$

$$\Gamma_{B+L} \simeq 250 \alpha_W^5 T \rightarrow 100 \lesssim T \lesssim 10^{12} \text{ GeV}$$



# Baryogenesis

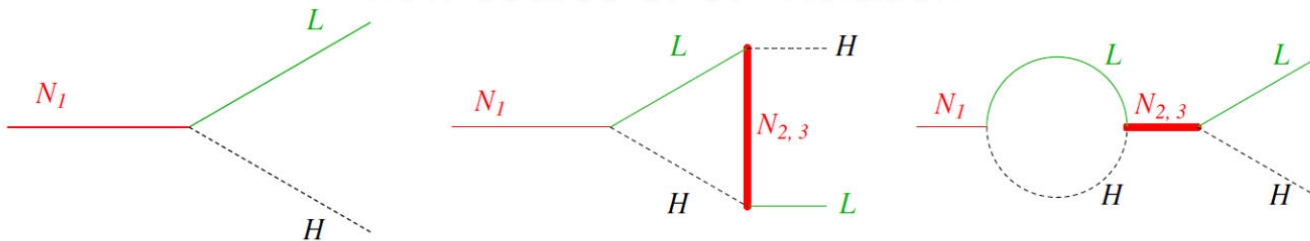
- Baryogenesis occurs at the boundary between different vacuum states (Kuzmin, Rubakov, Shaposhnikov '85 '86 '87)





# Leptogenesis

- A heavy neutrino decays out of equilibrium into leptons and anti-leptons unevenly (Fukugita, Yanagida '86)



A. Strumia, hep-ph/0608347 (2006)

$$\varepsilon_1 \equiv \frac{\Gamma(N_1 \rightarrow LH) - \Gamma(N_1 \rightarrow \bar{L}\bar{H})}{\Gamma(N_1 \rightarrow LH) + \Gamma(N_1 \rightarrow \bar{L}\bar{H})} \approx -\frac{3}{8\pi} \frac{1}{(hh^\dagger)_{11}} \sum_{i=2,3} \text{Im}(hh^\dagger)_{li}^2 \frac{M_1}{M_i}$$

$$\Delta L \neq 0 \rightarrow \text{sphalerons} \rightarrow \Delta B \neq 0$$

# Leptogenesis (Alternatives)

- Resonant leptogenesis
- Soft leptogenesis via oscillations
- Non-thermal leptogenesis
- CP-violation scattering
- $\nu$ -N Level-crossing
- .....

# Upper bound on baryogenesis scale from neutrino masses

Ann E. Nelson<sup>a,b,1,2</sup> and S.M. Barr<sup>a,c</sup>

<sup>a</sup> *Institute for Theoretical Physics, University of California, Santa Barbara, CA 93106, USA*

<sup>b</sup> *Department of Physics, University of California, San Diego, La Jolla, CA 92093, USA*

<sup>c</sup> *Bartol Research Institute, University of Delaware, Newark, DE 19716, USA*

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We examine the constraints on baryogenesis if anomalous weak baryon violation is in thermal equilibrium at high temperatures. If neutrinos have Majorana masses, there is an upper bound on the scale of baryogenesis:  $T_0 \leq 10^{12} \text{ GeV} (1 \text{ eV}/m_\nu)^2$ , where  $m_\nu$  is the mass of the *lightest* neutrino, and no baryon number is generated at temperatures below  $T_0$ .

# Chemical potential equilibrium

$$\begin{aligned}
 -\mu_q + \mu_H + \mu_{d_R} &= 0 \quad , \quad -\mu_q - \mu_H + \mu_{u_R} = 0 \quad , \quad -\mu_\ell + \mu_H + \mu_{e_R} = 0 \quad , \\
 3(3\mu_q + \mu_\ell) &= 0 \quad , \quad \mu_q + 2\mu_{u_R} - \mu_{d_R} - \mu_\ell - \mu_{e_R} + \frac{2}{3}\mu_H = 0 \quad ,
 \end{aligned}$$

All chemical potentials vanish after  $\Delta L=2$  kicks in !

$$\mu_\ell + \mu_H = 0$$

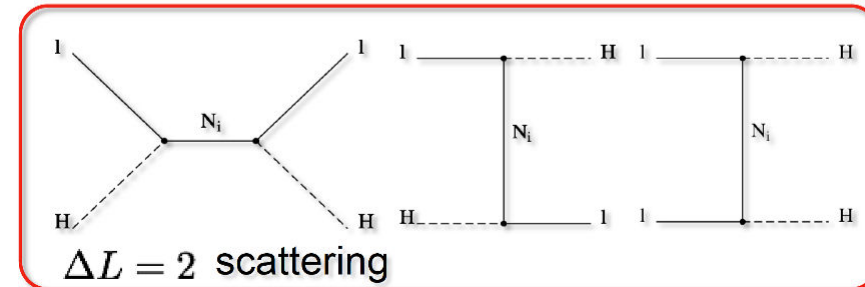
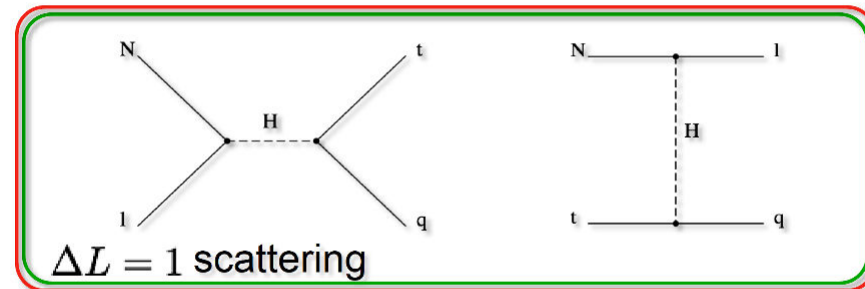
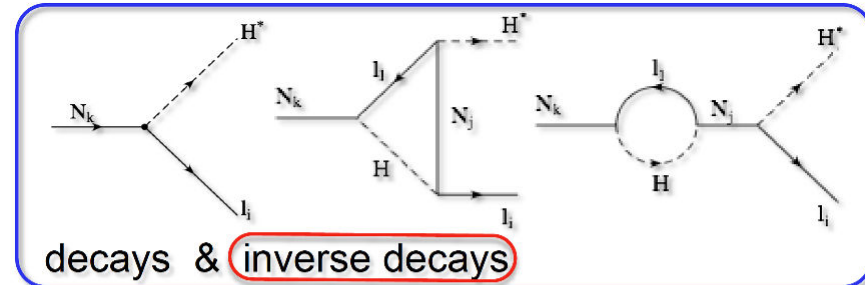
# Wash-out Effects on Leptogenesis

- Boltzmann equations describe evolution of  $N / L$  number density

$$Hz \frac{dN_{N_1}}{dz} = -(\Gamma_D + \Gamma_S)(N_{N_1} - N_{N_1}^{\text{eq}})$$

$$Hz \frac{dN_L}{dz} = \epsilon_1 \Gamma_D (N_{N_1} - N_{N_1}^{\text{eq}}) - \Gamma_W N_L$$

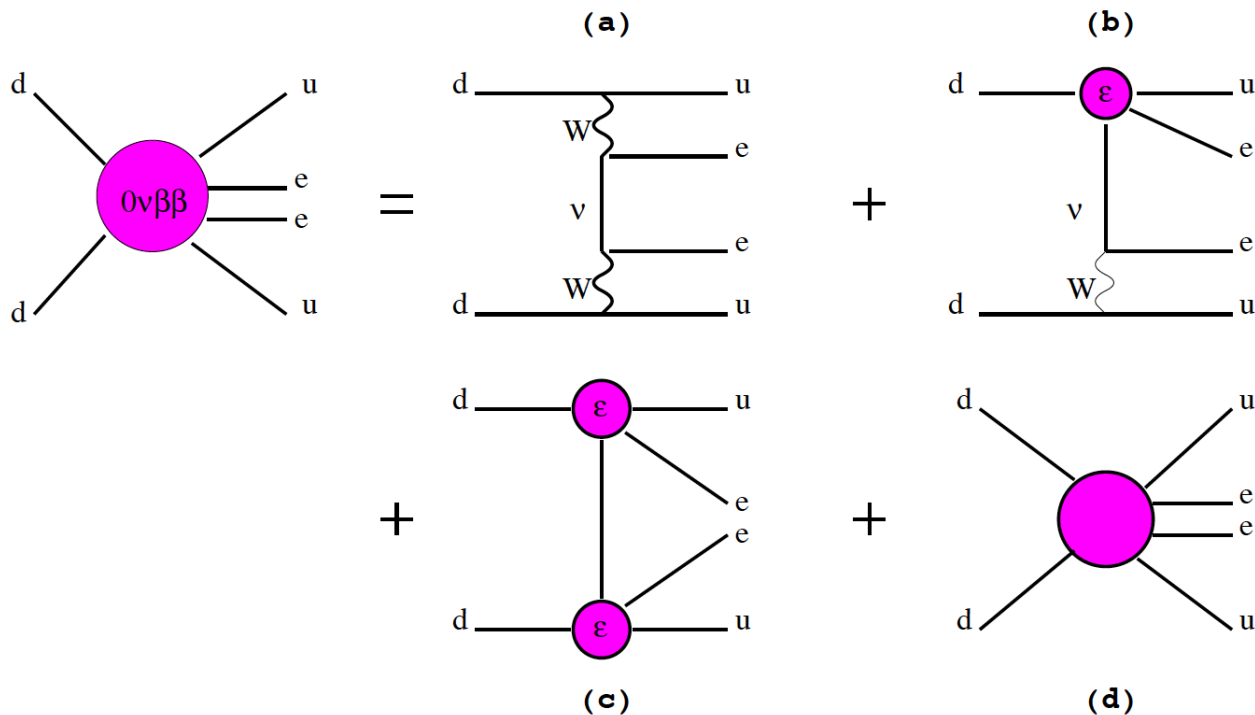
with  $z = \frac{M_{N_1}}{T}$



➤ L violation and the (L+B)-violating sphalerons erase both L and B

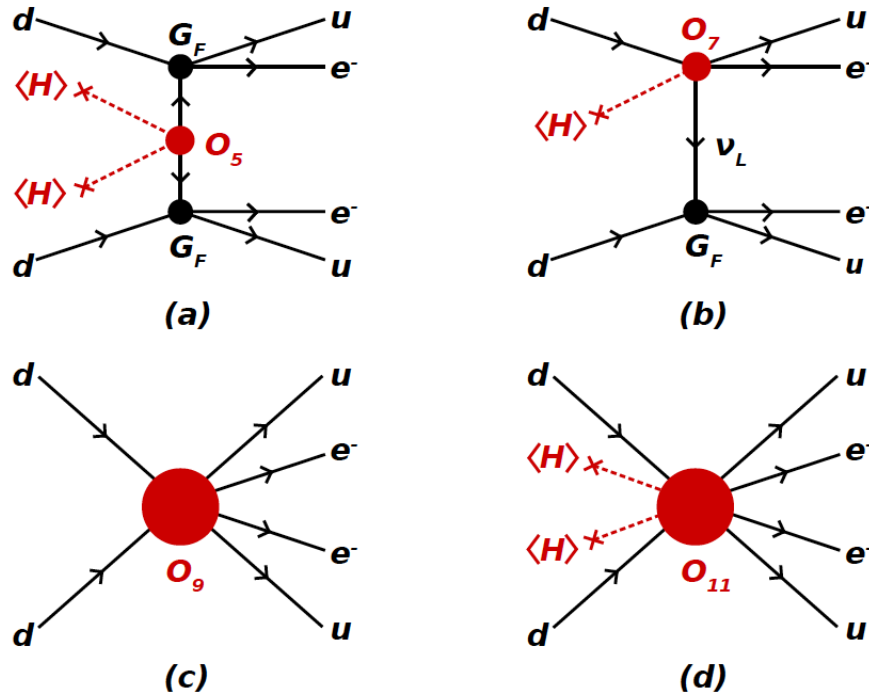
# Neutrinoless Double Beta Decay ( $0\nu\beta\beta$ )

- Lepton number is violated if  $0\nu\beta\beta$  is observed and SM neutrinos contains a Majorana component. It would wash out not only L and but also B in light of the sphalerons



# Lepton Number Violation (LNV)

## Operators



➤ We single out operators which contribute  $0\nu\beta\beta$  with short- and long-range interactions.

$$\mathcal{O}_5 = \frac{1}{\Lambda} (L^i L^j) H^k H^l \epsilon_{ik} \epsilon_{jl},$$

$$\mathcal{O}_7 = \frac{1}{\Lambda^3} (L^i d^c) (\bar{e}^c \bar{u}^c) H^j \epsilon_{ij},$$

$$\mathcal{O}_9 = \frac{1}{\Lambda^5} (L^i L^j) (\bar{Q}_i \bar{u}^c) (\bar{Q}_j \bar{u}^c),$$

$$\mathcal{O}_{11} = \frac{1}{\Lambda^7} (L^i L^j) (Q_k d^c) (Q_l d^c) H_m \bar{H}_i \epsilon_{jk} \epsilon_{lm},$$

FIG. 1: Contributions to  $0\nu\beta\beta$  decay generated by the operators in Eq. (2) in terms of effective vertices, point-like at the nuclear Fermi momentum scale.

# Lepton Flavor Violation (LFV)

- Since we only study wash-out effects resulting from the  $0\nu\beta\beta$  operators, only e-lepton asymmetry will be eliminated.
- In order to washout other flavor asymmetries, one would need LFV operators together with the  $0\nu\beta\beta$  operators.
- We study  $\ell_i \rightarrow \ell_j + \gamma$  and  $\ell_i \rightarrow \ell_j$  conversion

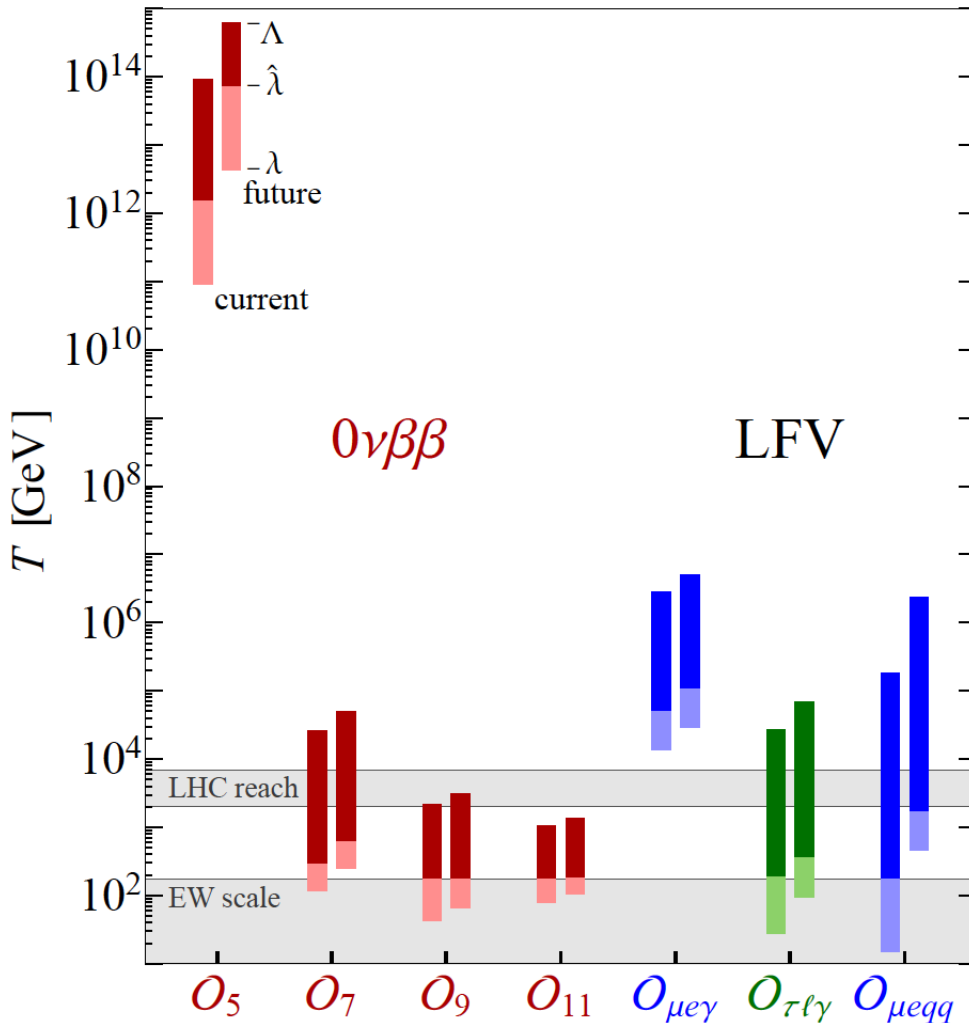
$$\mathcal{O}_{\ell\ell\gamma} = \mathcal{C}_{\ell\ell\gamma} \bar{L}_\ell \sigma^{\mu\nu} \bar{\ell}^c H F_{\mu\nu}$$

$$\mathcal{O}_{\ell\ell qq} = \mathcal{C}_{\ell\ell qq} (\bar{\ell} \Pi_1 \ell) (\bar{q} \Pi_2 q) \quad \mathcal{C}_{\ell\ell\gamma} = \frac{eg^3}{16\pi^2 \Lambda_{\ell\ell\gamma}^2}, \quad \mathcal{C}_{\ell\ell qq} = \frac{g^2}{\Lambda_{\ell\ell qq}^2},$$

$\Pi$  : Lorentz structures



# Results



- From , one can not differentiate  $O_9$  and  $O_{11}$  from  $O_5$
- However,  $O_9$  and  $O_{11}$  can be probed at the LHC

$$\mathcal{O}_5 = \frac{1}{\Lambda} (L^i L^j) H^k H^l \epsilon_{ik} \epsilon_{jl},$$

$$\mathcal{O}_7 = \frac{1}{\Lambda^3} (L^i d^c) (\bar{e}^c \bar{u}^c) H^j \epsilon_{ij},$$

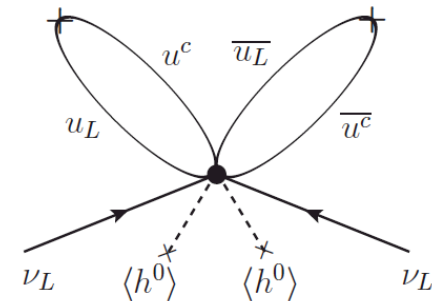
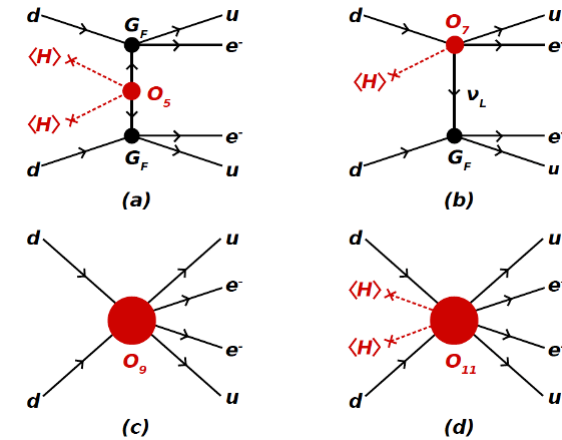
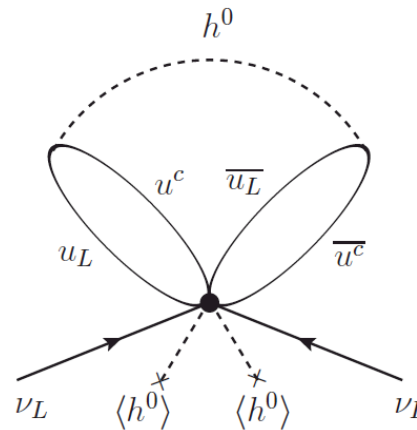
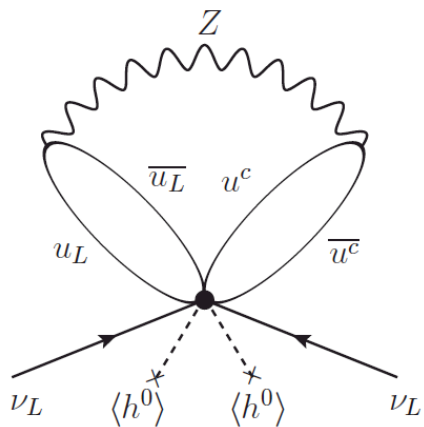
$$\mathcal{O}_9 = \frac{1}{\Lambda^5} (L^i L^j) (\bar{Q}_i \bar{u}^c) (\bar{Q}_j \bar{u}^c),$$

$$\mathcal{O}_{11} = \frac{1}{\Lambda^7} (L^i L^j) (Q_k d^c) (Q_l d^c) H_m \bar{H}_i \epsilon_{jklm},$$

# Tree- and loop-level contributions

- In the following, we try to find all contributions to  $0\nu\beta\beta$ , given an operator.

$$L^i L^j Q^k u^c \bar{Q}_l \bar{u}^c H^l H^m \epsilon_{ik} \epsilon_{jm}$$



# Automation

$f_L$	$\bar{f}_L$	$Z$	$g/(16\pi^2)$
$f_L$	$\bar{f}'_L$	$W^-$	$g/(16\pi^2)$
$\bar{f}^c$	$\bar{f}'_L$	$H^-$	$y_f/(16\pi^2)$
$\bar{f}^c$	$\bar{f}_L$	$h^0$	$y_f/(16\pi^2)$
$Z$	$\bar{f}_L$	$\bar{f}_L$	$g/(16\pi^2)$
$W^-$	$\bar{f}_L$	$\bar{f}'_L$	$g/(16\pi^2)$
$H^-$	$f^c$	$\bar{f}'_L$	$y_f/(16\pi^2)$
$h^0$	$\bar{f}_L$	$f^c$	$y_f/(16\pi^2)$
$\langle h \rangle$	$\bar{f}_L$	$f^c$	$vy_f/(16\pi^2)$
$h^0 W^- H^-$	$\bar{h}^0 W^+ H^+$	—	$1/(16\pi^2)$

$f_L$	$f^c$	$h^0$	$y_f/(16\pi^2)^2$		
$f^c$	$f'_L$	$H^+$	$y_f/(16\pi^2)^2$		
$f_L$	$\bar{f}'_L$	$W^+$	$g/(16\pi^2)^2$		
$f_L$	$\bar{f}_L$	$Z$	$g/(16\pi^2)^2$		
$h$	$Z$	$ W^+$	$Z$	$ W^-$	$vg^2/(16\pi^2)^2$
$Z$	$H^+ W^+$	$W^- H^-$	$2vg^2/(16\pi^2)^2$		

# Operator lists

$\mathcal{O}$	Operator	$m_\nu$	LR	$\epsilon_{\text{LR}}$
$1^{H^2}$	$L^i L^j H^k H^l \bar{H}^t H_t \epsilon_{ik} \epsilon_{jl}$	$\frac{v^2}{\Lambda} f\left(\frac{v}{\Lambda}\right)$	—	—
2	$L^i L^j L^k e^c H^l \epsilon_{ij} \epsilon_{kl}$	$\frac{y_e}{16\pi^2} \frac{v^2}{\Lambda}$	—	—
$3_a$	$L^i L^j Q^k d^c H^l \epsilon_{ij} \epsilon_{kl}$	$\frac{y_d g^2}{(16\pi^2)^2} \frac{v^2}{\Lambda}$	$\frac{v}{\Lambda^3}$	$\epsilon_{S+P}^{S+P}$
$3_b$	$L^i L^j Q^k d^c H^l \epsilon_{ik} \epsilon_{jl}$	$\frac{y_d}{16\pi^2} \frac{v^2}{\Lambda}$	$\frac{v}{\Lambda^3}$	$\epsilon_{S+P}^{S+P}$
$4_a$	$L^i L^j \bar{Q}_i \bar{u}^c H^k \epsilon_{jk}$	$\frac{y_u}{16\pi^2} \frac{v^2}{\Lambda}$	$\frac{v}{\Lambda^3}$	$\epsilon_{S-P}^{S+P}$
$4_b^*$	$L^i L^j \bar{Q}_k \bar{u}^c H^k \epsilon_{ij}$	$\frac{y_u g^2}{(16\pi^2)^2} \frac{v^2}{\Lambda}$	$\frac{v}{\Lambda^3}$	$\epsilon_{S-P}^{S+P}$
8	$L^i \bar{e}^c \bar{u}^c d^c H^j \epsilon_{ij}$	$\frac{y_e^{\text{ex}} y_d y_u}{(16\pi^2)^2} \frac{v^2}{\Lambda}$	$\frac{v}{\Lambda^3}$	$2\epsilon_{V+A}^{V+A}$

Table 4: Effective  $\Delta L = 2$  SM operators at dimension 7. Dominant contributions to  $0\nu\beta\beta$  decay via the effective neutrino mass ( $m_\nu$ ) and long-range (LR) mechanisms are shown. The  $0\nu\beta\beta$  long-range interaction excited by a particular operator is denoted in column  $\epsilon_{\text{LR}}$ . The notation of the contributions is explained in Sec. 4.3.

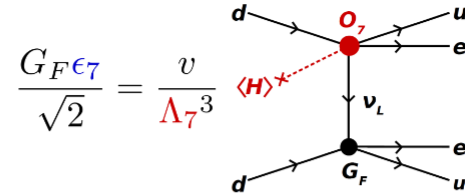


# Comparison

## Why is it of interest?

### Dependence on experimental sensitivity

$\mathcal{O}_7^{3a} = L^i L^j Q^k d^c H^l \epsilon_{ij} \epsilon_{kl}$	}	$e_L \nu_L u_L d^c$	→	$\epsilon_{S+P}^{S+P}$
$\mathcal{O}_7^{3b} = L^i L^j Q^k d^c H^l \epsilon_{ik} \epsilon_{jl}$				
$\mathcal{O}_9^5 = L^i L^j Q^k d^c H^l H^m \bar{H}_i \epsilon_{jl} \epsilon_{km}$				
$\mathcal{O}_7^{4a} = L^i L^j \bar{Q}_i \bar{u}^c H^k \epsilon_{jk}$	}	$e_L \nu_L \bar{d}_L \bar{u}^c$	→	$\epsilon_{S-P}^{S+P}$
$\mathcal{O}_7^{4b} = L^i L^j \bar{Q}_k \bar{u}^c H^k \epsilon_{ij}$				
$\mathcal{O}_9^6 = L^i L^j \bar{Q}_k \bar{u}^c H^l H^k \bar{H}_i \epsilon_{jl}$				
$\mathcal{O}_9^7 = L^i Q^j \bar{e}^c \bar{Q}_k H^k H^l H^m \epsilon_{il} \epsilon_{jm}$	}	$\nu_L u_L \bar{e}^c \bar{d}_L$	→	$\frac{1}{2} \epsilon_{V-A}^{V+A}$
$\mathcal{O}_7^8 = L^i \bar{e}^c \bar{u}^c d^c H^j \epsilon_{ij}$				
		$\nu_L \bar{e}^c \bar{u}^c d^c$	→	$\frac{1}{2} \epsilon_{V+A}^{V+A}$



$$\frac{G_F \epsilon_7}{\sqrt{2}} = \frac{v}{\Lambda_7^3}$$

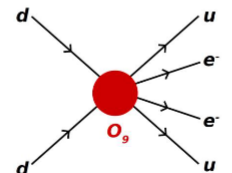
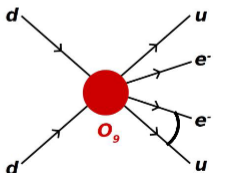
Isotope	$ \epsilon_{V-A}^{V+A} $	$ \epsilon_{V+A}^{V+A} $	$ \epsilon_{S-P}^{S+P} $	$ \epsilon_{S+P}^{S+P} $	$ \epsilon_{TL}^{TR} $	$ \epsilon_{TR}^{TR} $
<sup>76</sup> Ge	$3.3 \cdot 10^{-9}$	$5.9 \cdot 10^{-7}$	$1.0 \cdot 10^{-8}$	$1.0 \cdot 10^{-8}$	$6.4 \cdot 10^{-10}$	$1.0 \cdot 10^{-9}$
<sup>136</sup> Xe	$2.6 \cdot 10^{-9}$	$5.1 \cdot 10^{-7}$	$6.2 \cdot 10^{-9}$	$6.2 \cdot 10^{-9}$	$4.4 \cdot 10^{-10}$	$7.4 \cdot 10^{-10}$

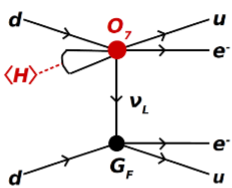
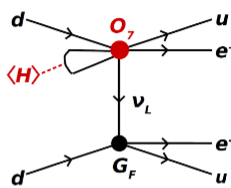
F. Deppisch, M. Hirsch, H. Päs, J. Phys. G 39 (2012) 124007, arXiv:1208.0727 [hep-ph], updated

# Comparison

## Why is it of interest?

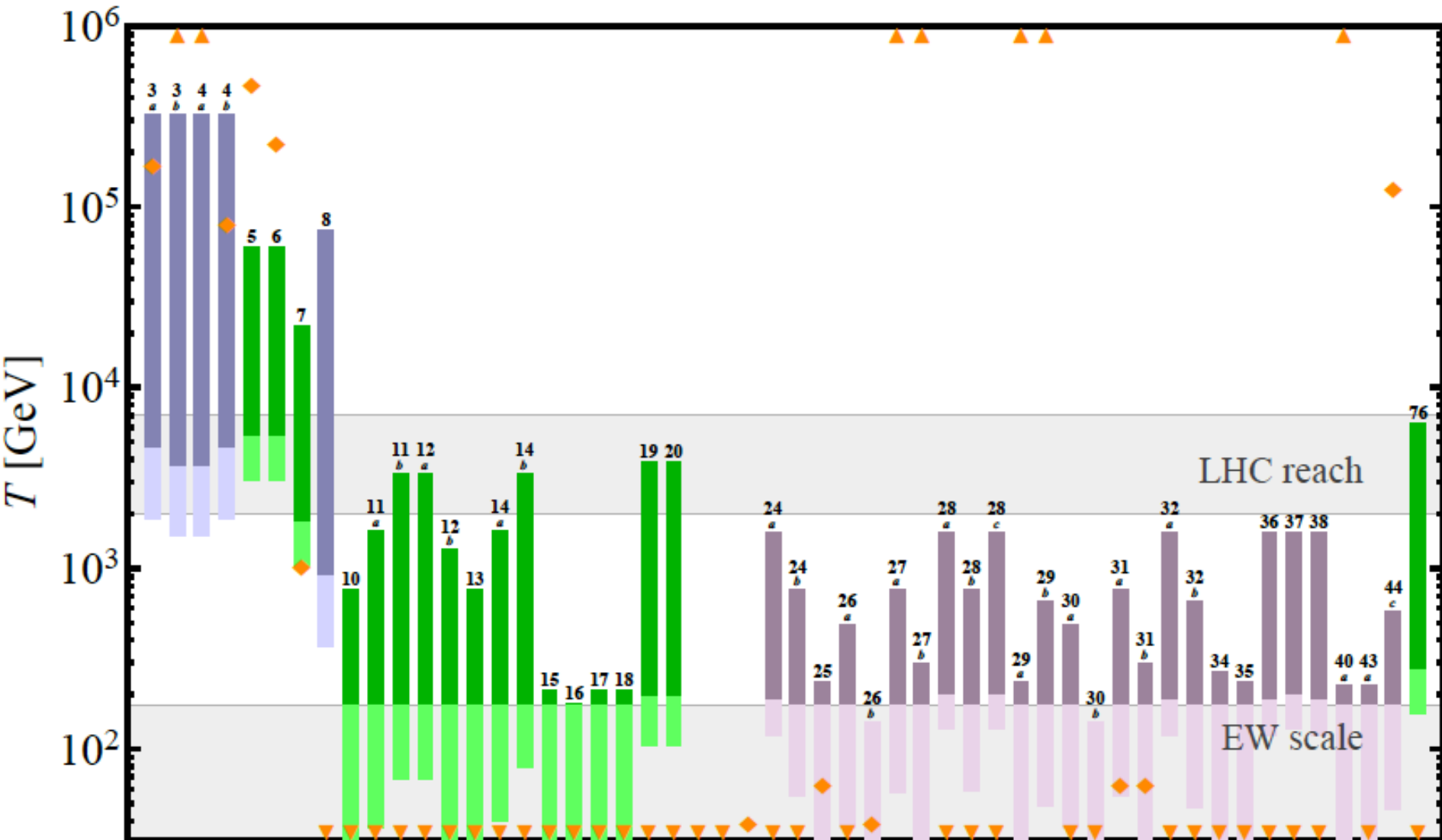
### Crucial dependence on SU(2) structure and Yukawa couplings

$\mathcal{O}_9^{11b} = L^i L^j Q^k d^c Q^l d^c \epsilon_{ik} \epsilon_{jl}$ $\frac{G_F^2 \epsilon_9}{2m_p} = \frac{1}{\Lambda_9^5}$  <p style="text-align: center; color: red;"><b>at tree level</b></p>	$\mathcal{O}_9^{11a} = L^i L^j Q^k d^c Q^l d^c \epsilon_{ij} \epsilon_{kl}$ $\frac{G_F^2 \epsilon_9}{2m_p} = \frac{g^2}{16\pi^2 \Lambda_9^5}$ <p style="text-align: center; color: red;"><i>(flavour structure!)</i></p>  <p style="text-align: center; color: red;"><b>only at one loop</b></p>
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$\mathcal{O}_9^{11b} = L^i L^j Q^k d^c Q^l d^c \epsilon_{ik} \epsilon_{jl}$ $\frac{G_F \epsilon_7}{\sqrt{2}} = \frac{y_d v}{16\pi^2 \Lambda_9^3}$ 	<p style="text-align: center; color: red;"><b>same</b></p> $\mathcal{O}_9^{11a} = L^i L^j Q^k d^c Q^l d^c \epsilon_{ij} \epsilon_{kl}$ $\frac{G_F \epsilon_7}{\sqrt{2}} = \frac{y_d v}{16\pi^2 \Lambda_9^3}$ 
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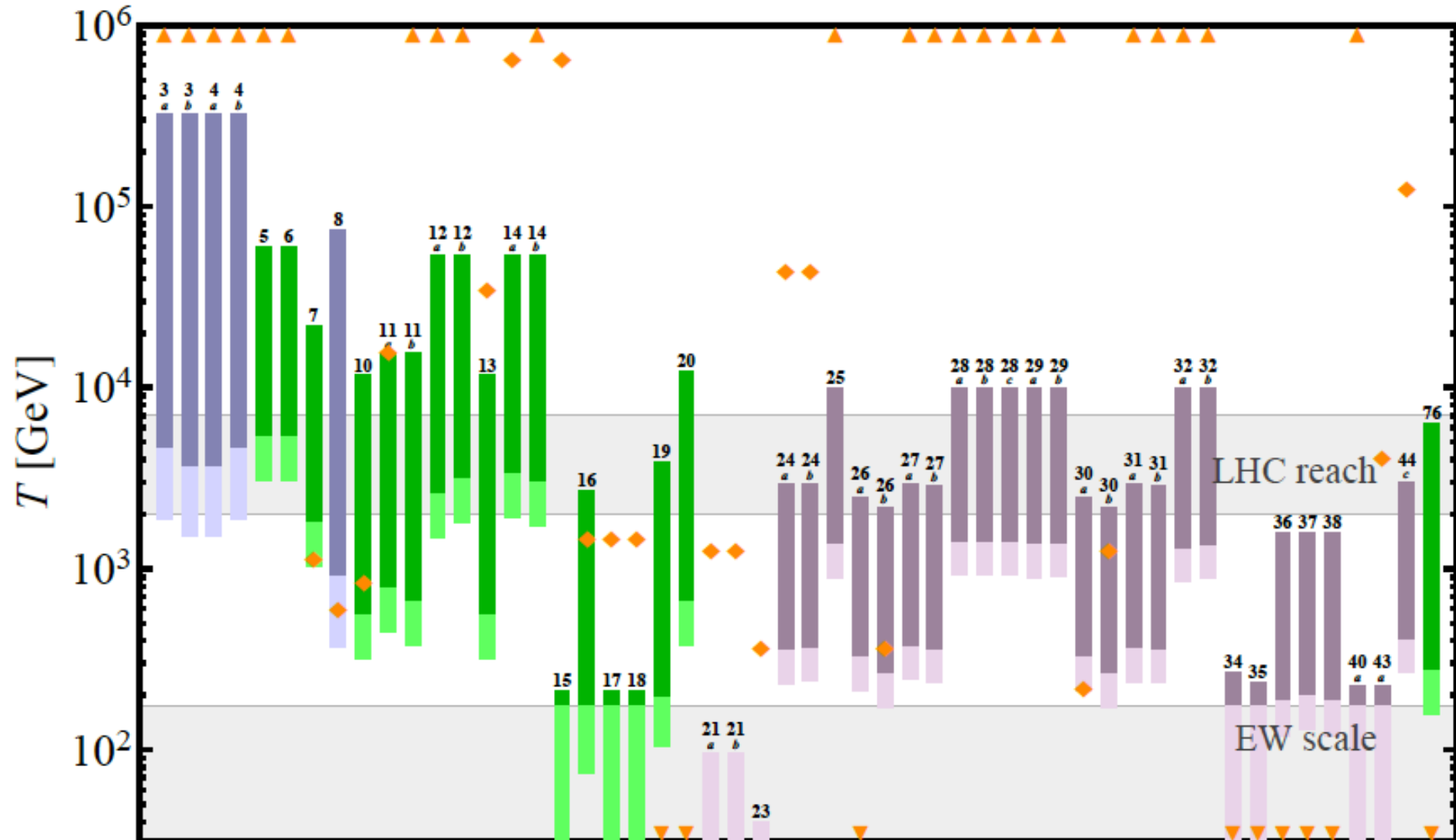
$\mathcal{O}_9^{20} = L^i d^c \bar{Q}_i \bar{u}^c \bar{e}^c \bar{u}^c$ $\frac{G_F^2 \epsilon_9}{2m_p} = \frac{1}{\Lambda_9^5}$ 	$\frac{G_F \epsilon_7}{\sqrt{2}} = \frac{y_u v}{(16\pi^2) \Lambda_9^3}$
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# Results (1<sup>st</sup> Gen)





# Results (3<sup>rd</sup> Gen)



# Beyond EFT approach

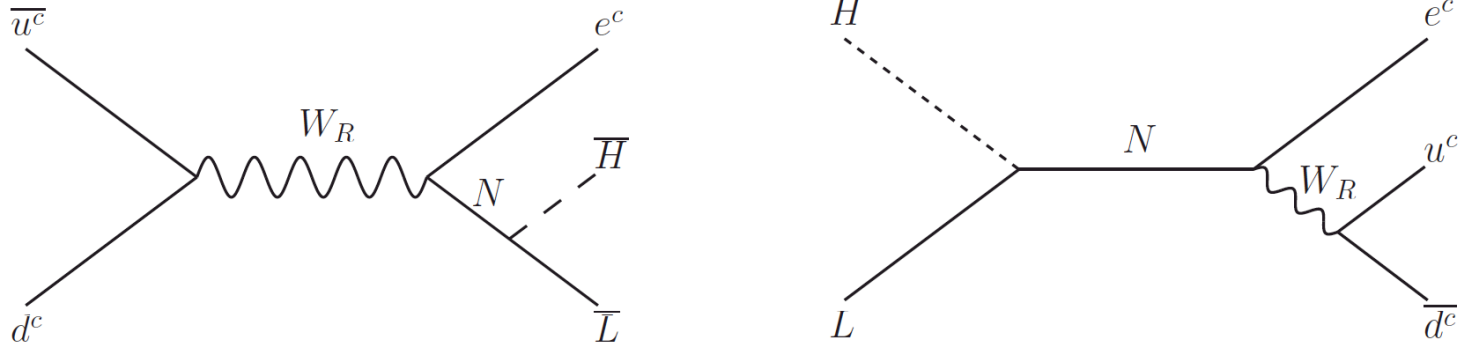
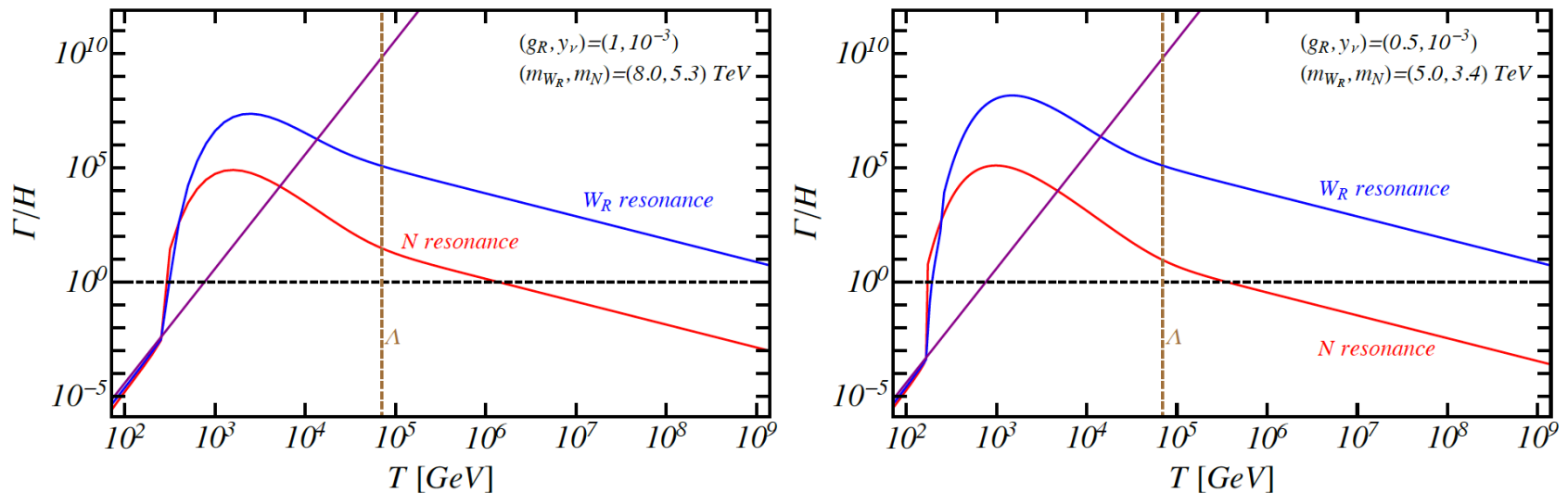


Figure 19: Two example diagrams in a left-right symmetric model framework that give rise to the effective operator  $\mathcal{O}_8 = L^i \bar{e}^c \bar{u}^c d^c H^j \epsilon_{ij}$ .



# Caveats

- $0\nu\beta\beta$  decays only probe the electron flavor, so LFV is needed to wash out asymmetries stored in  $\mu$  and  $\tau$  flavors
- To carry out the analysis in a model-independent way, we assume no correlation between the generation mechanism and washout
- The existence of a decoupled sector can protect asymmetries from washout in the visible sectors (Phys. Lett. B207, 210 (1988) and 1309.4770)



# Can ADM save world?

$$\begin{aligned}
 & -\mu_q + \mu_H + \mu_{d_R} = 0 \quad , \quad -\mu_q - \mu_H + \mu_{u_R} = 0 \quad , \quad -\mu_\ell + \mu_H + \mu_{e_R} = 0 \quad , \\
 & 3(3\mu_q + \mu_\ell) = 0 \quad , \quad \mu_q + 2\mu_{u_R} - \mu_{d_R} - \mu_\ell - \mu_{e_R} + \frac{2}{3}\mu_H = 0 \quad ,
 \end{aligned}$$

All chemical potentials vanish after  $\Delta L=2$  kicks in !

$$\mu_\ell + \mu_H = 0$$

# Can ADM save world?

$$\begin{aligned}
 & -\mu_q + \mu_H + \mu_{d_R} = 0 \quad , \quad -\mu_q - \mu_H + \mu_{u_R} = 0 \quad , \quad -\mu_\ell + \mu_H + \mu_{e_R} = 0 \quad , \\
 & \cancel{3(3\mu_q + \mu_\ell) = 0} \quad , \quad \mu_q + 2\mu_{u_R} - \mu_{d_R} - \mu_\ell - \mu_{e_R} + \frac{2}{3}\mu_H = 0 \quad ,
 \end{aligned}$$

$$\mu_\ell + \mu_H = 0 \quad ,$$

If particles in the dark sector are also charged under  $SU(2)_L$ , then the sphalerons can transfer symmetry between B, L and X (dark charge) => Asymmetric DM

$$3(3\mu_q + \mu_\ell) + n_X\mu_X = 0,$$

# Can ADM save world?

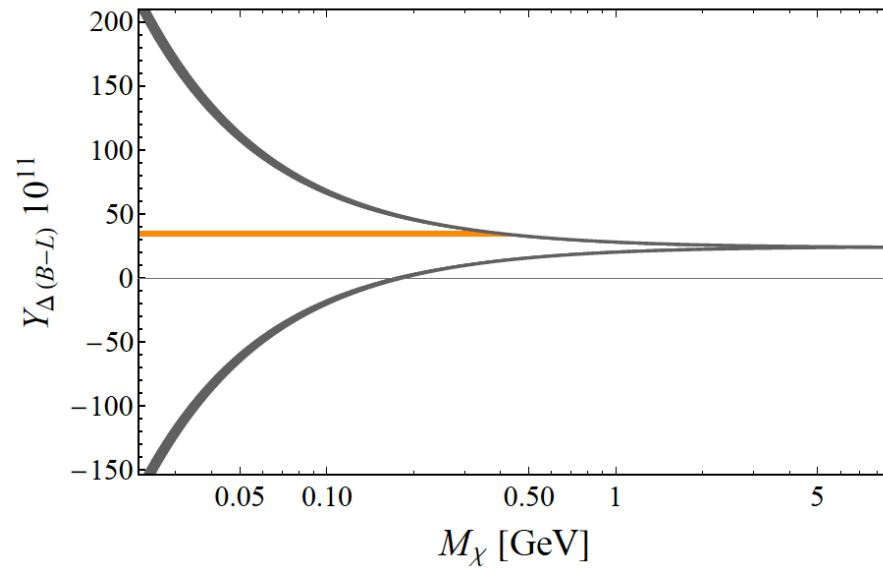
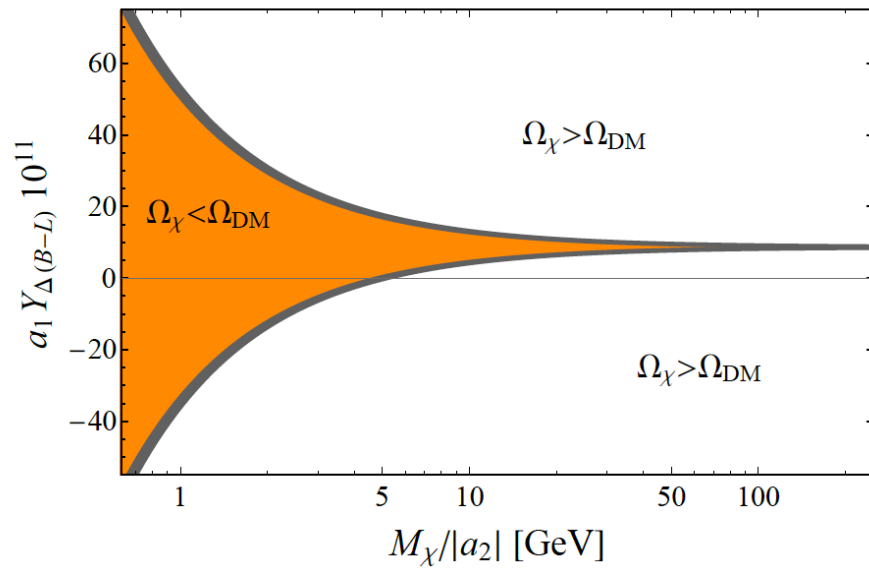
$$\begin{aligned}
 -\mu_q + \mu_H + \mu_{d_R} &= 0 \quad , \quad -\mu_q - \mu_H + \mu_{u_R} = 0 \quad , \quad -\mu_\ell + \mu_H + \mu_{e_R} = 0 \quad , \\
 3(3\mu_q + \mu_\ell) &= 0 \quad , \quad \mu_q + 2\mu_{u_R} - \mu_{d_R} - \mu_\ell - \mu_{e_R} + \frac{2}{3}\mu_H = 0 \quad , \\
 \mu_\ell + \mu_H &= 0 \quad ,
 \end{aligned}$$

If models need an extra asymmetry-transfer interaction, then DM asymmetry will also vanish!

$$X_{\text{DM}}^2 (\ell H)^2 \quad , \quad X_{\text{DM}} d_R d_R u_R \quad (\text{or } X_{\text{DM}}^2 d_R d_R u_R)$$

# Can ADM save world?

$$Y_{\Delta B} = a_1 Y_{\Delta(B-L)} + a_2 Y_{\Delta X} \quad \longrightarrow \quad M_\chi \leq M_p \frac{|a_2|}{\left|1 - a_1 \frac{Y_{\Delta(B-L)}}{Y_{\Delta B}}\right|} \frac{\Omega_{\text{DM}}}{\Omega_B}$$



$$Y_{\Delta L} = a_2 a_3 Y_{\Delta X}$$



# Conclusions and Outlook

- Observation of LNV via  $0\nu b\bar{b}$  decay or at colliders together with LFV can falsify high-scale baryogenesis/leptogenesis
- A single LNV operator may induce at tree- and loop-level to short- and long-range contributions to  $0\nu b\bar{b}$  decay
- In certain ADM models, the existence of DM can *revive* high-scale baryon or lepton asymmetry generation mechanisms and realize the connection of the baryon and DM density