

		Second letter				
		U	C	A	G	
First letter	U	UUU } Phe UUC } UUA } Leu UUG }	UCU } UCC } Ser UCA } UCG }	UAU } Tyr UAC } UAA Stop UAG Stop	UGU } Cys UGC } UGA Stop UGG Trp	U C A G
	C	CUU } CUC } Leu CUA } CUG }	CCU } CCC } Pro CCA } CCG }	CAU } His CAC } CAA } Gln CAG }	CGU } CGC } Arg CGA } CGG }	U C A G
	A	AUU } AUC } Ile AUA } AUG Met	ACU } ACC } Thr ACA } ACG }	AAU } Asn AAC } AAA } Lys AAG }	AGU } Ser AGC } AGA } Arg AGG }	U C A G
	G	GUU } GUC } Val GUA } GUG }	GCU } GCC } Ala GCA } GCG }	GAU } Asp GAC } GAA } Glu GAG }	GGU } GGC } Gly GGA } GGG }	U C A G



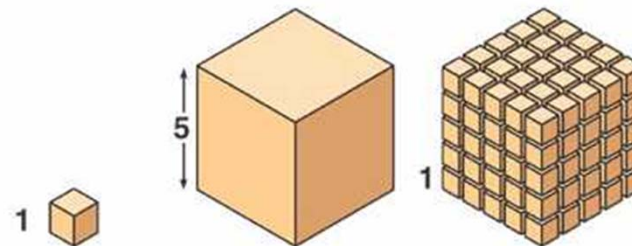
Nanomaterials

- Metals and Alloys
 - Fe, Al, Au
- Semiconductors
 - Band gap, CdS, TiO₂, ZnO
- Ceramic
 - Al₂O₃, Si₃N₄, MgO, , SiO₂, ZrO₂
- Carbon based
 - Diamond, graphite, nanotube, C60, graphene
- Polymers
 - Soft mater, block co-polymer
- Biological
 - Photonic, hydrophobic, adhesive,
- Composites



Surface to Volume Ratio

Surface area increases while
total volume remains constant



Total surface area (height \times width \times number of sides \times number of boxes)	6	150	750
Total volume (height \times width \times length \times number of boxes)	1	125	125
Surface-to-volume ratio (surface area \div volume)	6	1.2	6



Surface to Volume Ratio

Au: AAA

Atomic mass: 196.967

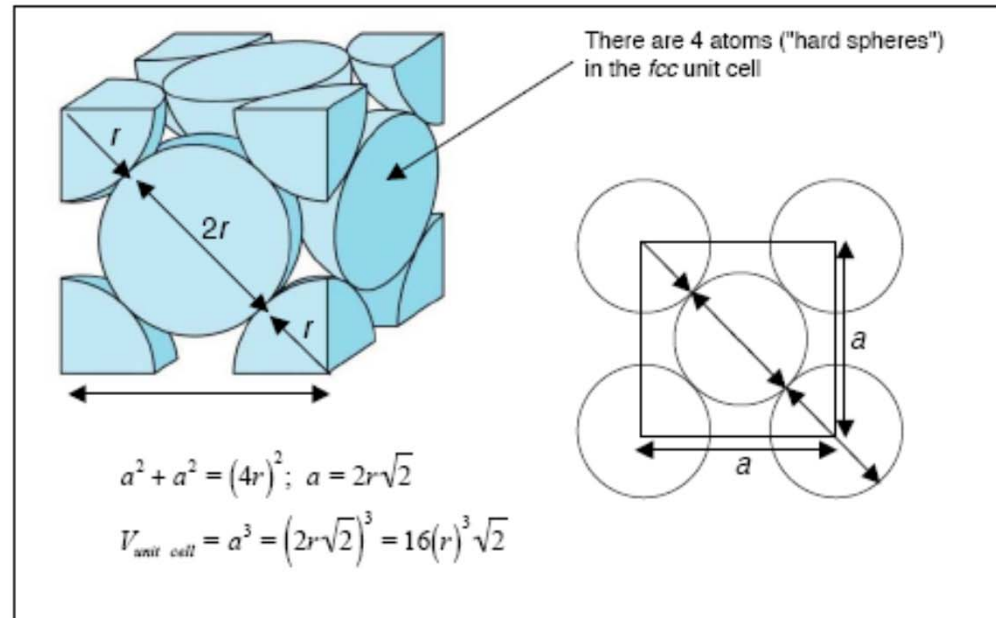
Density 19.31

Radii = 0.144 nm

Number of Au atoms in 1 m	$3.4 \cdot 10^9$
Volume of Au atom	$4.19 \cdot 10^{-28}$
Surface area Au atom	$7.22 \cdot 10^{-19}$
Surface/volume ratio	$1.72 \cdot 10^9$



fcc



$$V_{\text{unit cell}} = a^3 = (2r\sqrt{2})^3 = 16(0.5\text{nm})^3\sqrt{2} = 2.828 \text{ nm}^3$$

$$\frac{10^{27} \text{ nm}^3}{2.828 \text{ nm}^3} = 3.536 \times 10^{26} \text{ nano unit cells}$$

$$\frac{S_{\text{spheres}}}{S_{\text{unit cell}}} = \frac{4.44 \times 10^9 \text{ m}^2}{6.0 \times 10^9 \text{ m}^2} = 0.74$$

$$\text{Collective Area} = 3.536 \times 10^{26} \text{ nano unit cells} \left(\frac{4 \text{ spheres}}{\text{unit cell}} \right) \left(\frac{4\pi r^2}{\text{sphere}} \right) = 4.44 \times 10^{27} \text{ nm}^2$$



Packing Fraction

$$\text{APF} = \frac{N_{\text{atoms}} V_{\text{atom}}}{V_{\text{crystal}}}$$

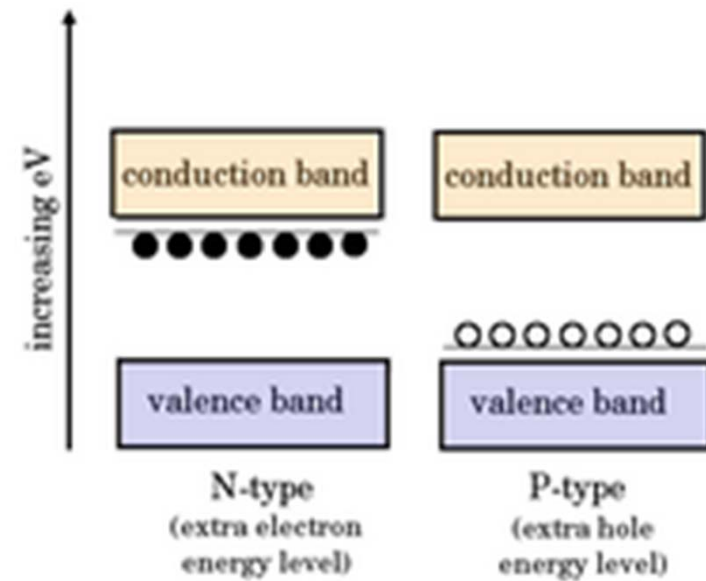
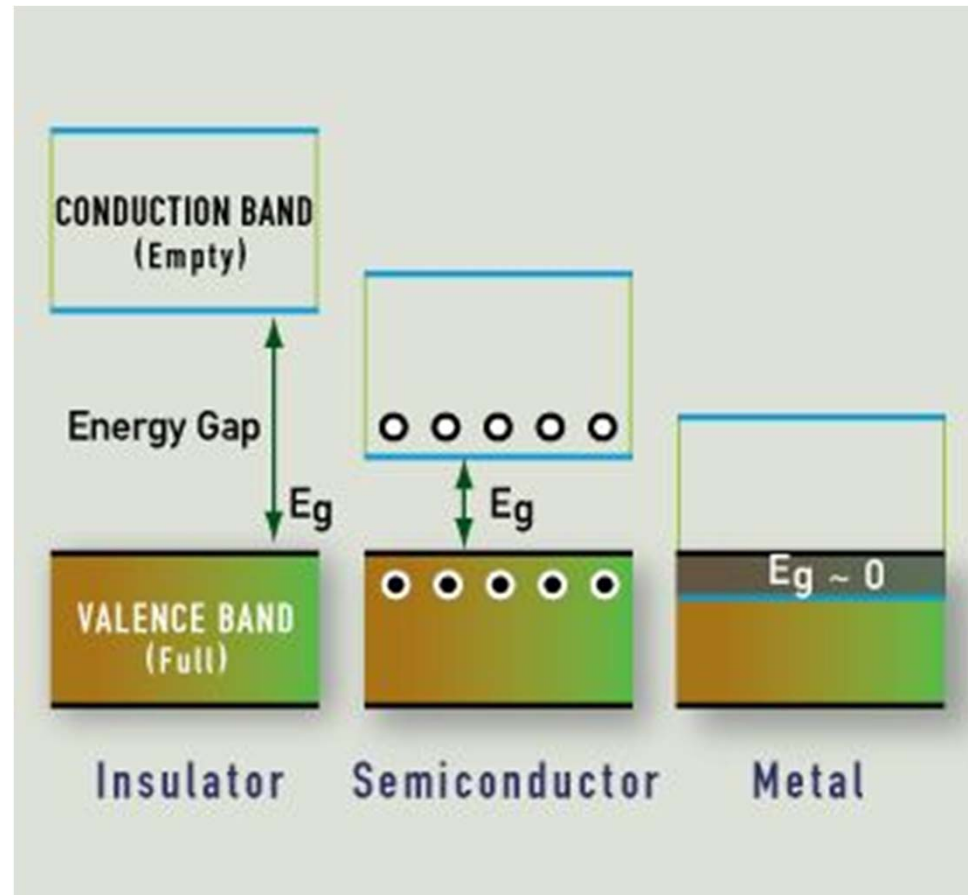


Surfaces

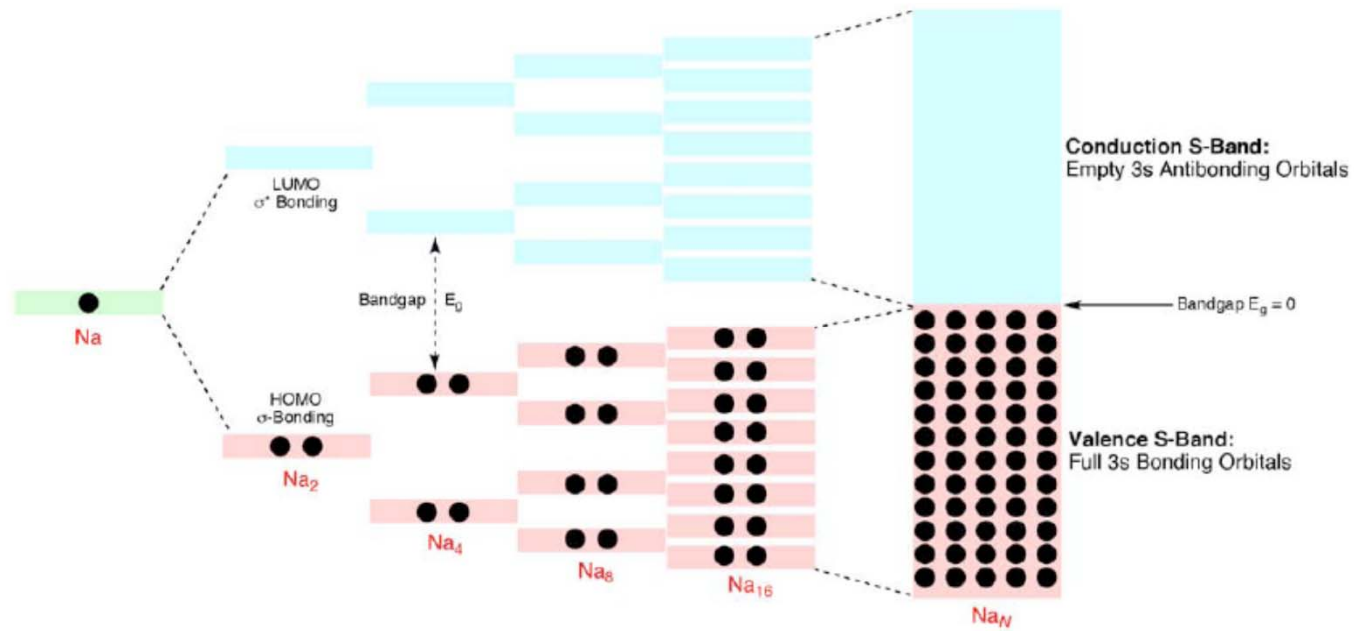
- Collective surface area of nanocube 1 nm
- Porous materials
 - Micropore (<2 nm)
 - Mesopore (2 nm ~ 50 nm)
 - Marcopore (> 50nm)
- Void volume
 - $V_{\text{pore}}/V_{\text{material}}$



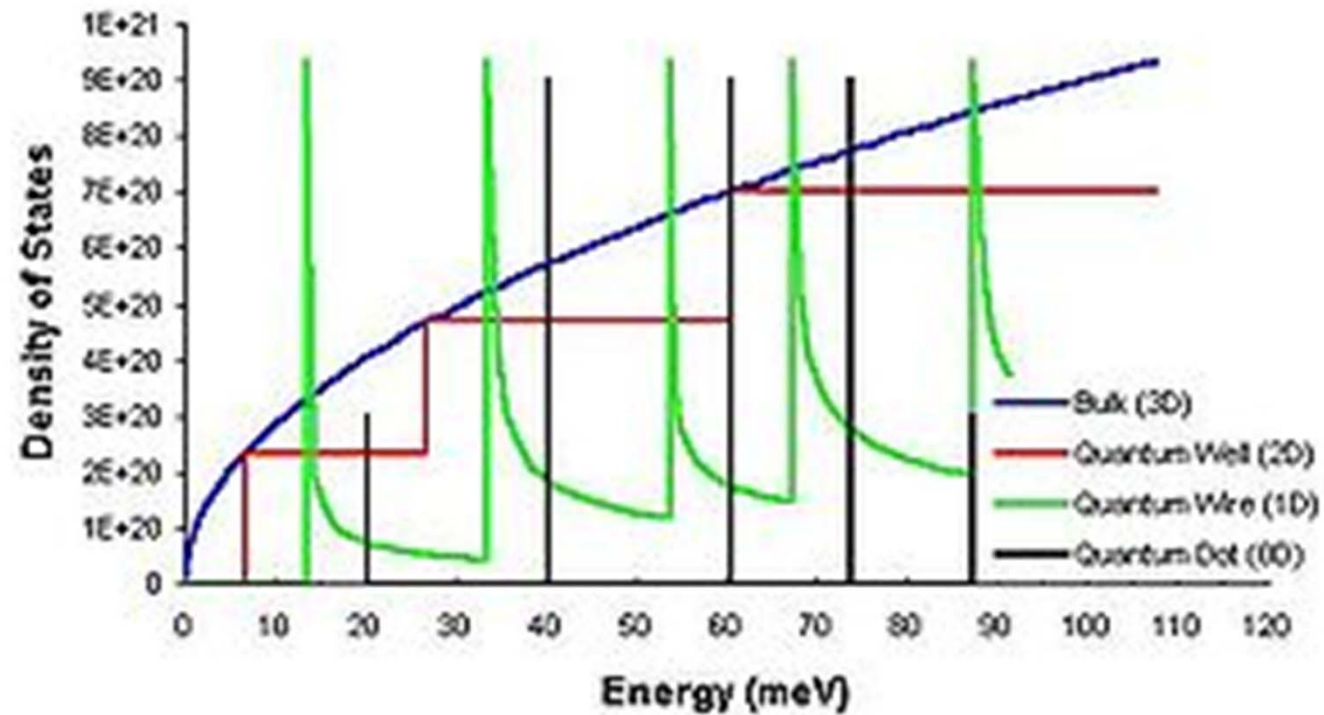
Bandgap



Bandgap



Density of State

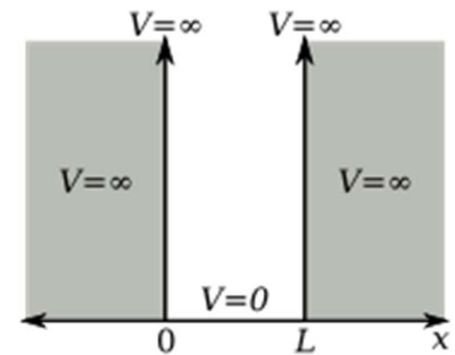


Particle in a Box

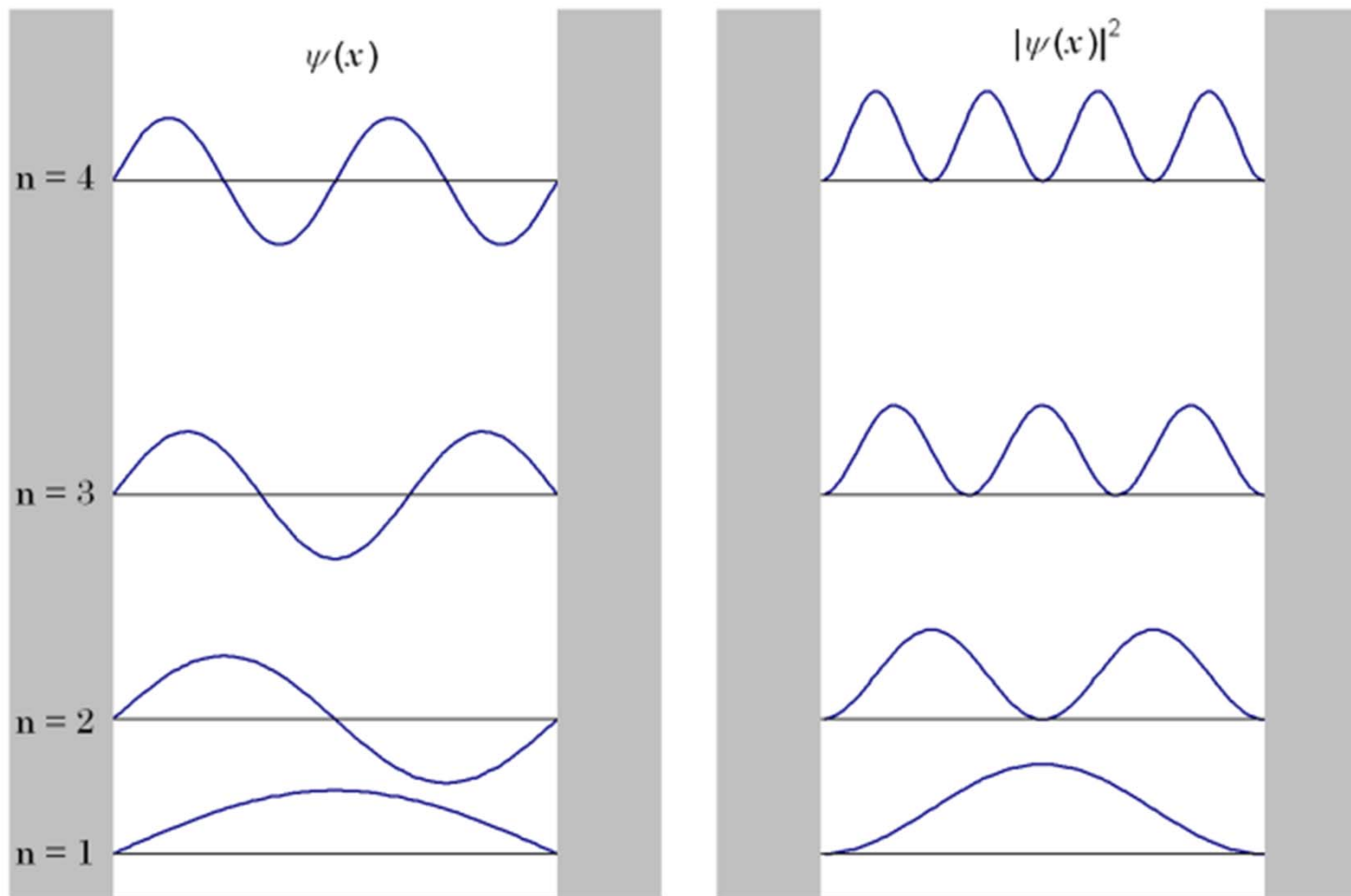
$$-\frac{\hbar^2}{2m} \frac{d^2\psi(x)}{dx^2} + V(x)\psi(x) = E\psi(x) \quad (1)$$

$$\psi_n = \sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right)$$

$$E_n = \frac{\hbar^2 \pi^2}{2mL^2} n^2$$



Particle in a Box



$$\psi_{n_x, n_y} = \sqrt{\frac{4}{L_x L_y}} \sin\left(\frac{n_x \pi x}{L_x}\right) \sin\left(\frac{n_y \pi y}{L_y}\right)$$

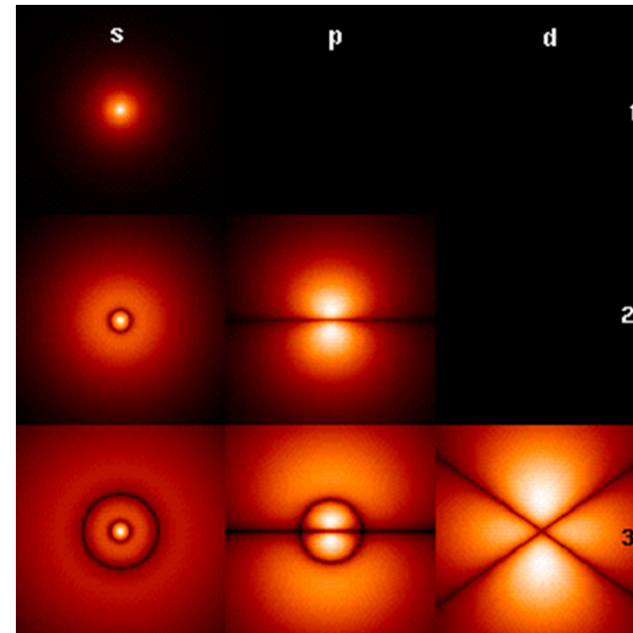
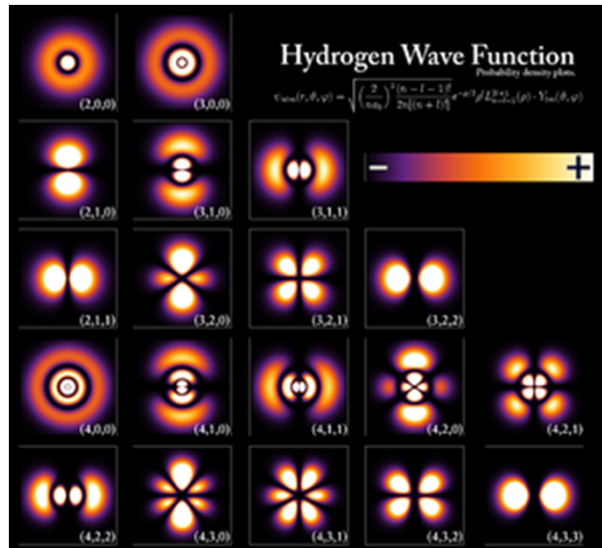
$$E_{n_x, n_y} = \frac{\hbar^2 \pi^2}{2m} \left[\left(\frac{n_x}{L_x}\right)^2 + \left(\frac{n_y}{L_y}\right)^2 \right]$$

$$\psi_{n_x, n_y, n_z} = \sqrt{\frac{8}{L_x L_y L_z}} \sin\left(\frac{n_x \pi x}{L_x}\right) \sin\left(\frac{n_y \pi y}{L_y}\right) \sin\left(\frac{n_z \pi z}{L_z}\right) \quad (22)$$

$$E_{n_x, n_y, n_z} = \frac{\hbar^2 \pi^2}{2m} \left[\left(\frac{n_x}{L_x}\right)^2 + \left(\frac{n_y}{L_y}\right)^2 + \left(\frac{n_z}{L_z}\right)^2 \right] \quad (23)$$



Wave Functions



$$i\hbar \frac{\partial}{\partial t} \Psi(\mathbf{r}, t) = \hat{H} \Psi = \left(-\frac{\hbar^2}{2m} \nabla^2 + V(\mathbf{r}) \right) \Psi(\mathbf{r}, t) = -\frac{\hbar^2}{2m} \nabla^2 \Psi(\mathbf{r}, t) + V(\mathbf{r}) \Psi(\mathbf{r}, t)$$

$$V(r) = -\frac{1}{4\pi\epsilon_0} \frac{Ze^2}{r}$$

$$\psi_{n\ell m}(r, \vartheta, \varphi) = \sqrt{\left(\frac{2}{na_0}\right)^3 \frac{(n-\ell-1)!}{2n(n+\ell)!}} e^{-\rho/2} \rho^\ell L_{n-\ell-1}^{2\ell+1}(\rho) \cdot Y_\ell^m(\vartheta, \varphi)$$

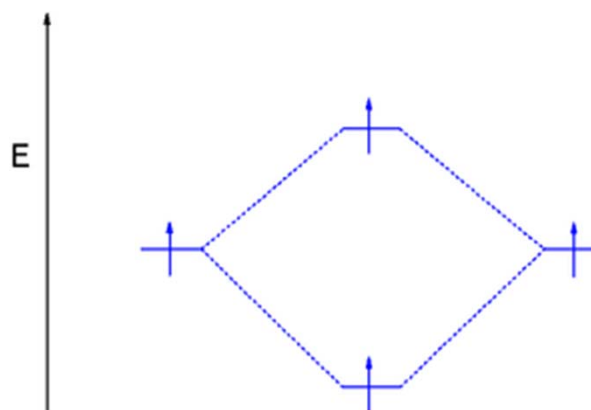


Linear combination of atomic orbitals molecular orbital method

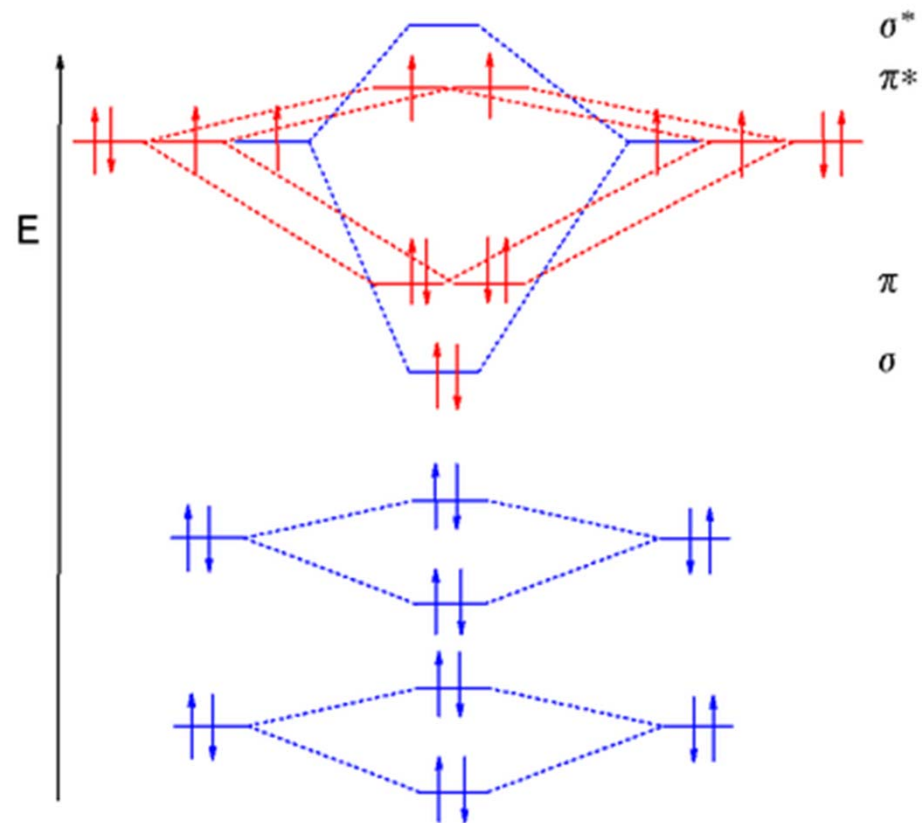
$$\phi_i = c_{1i}\chi_1 + c_{2i}\chi_2 + c_{3i}\chi_3 + \cdots + c_{ni}\chi_n$$

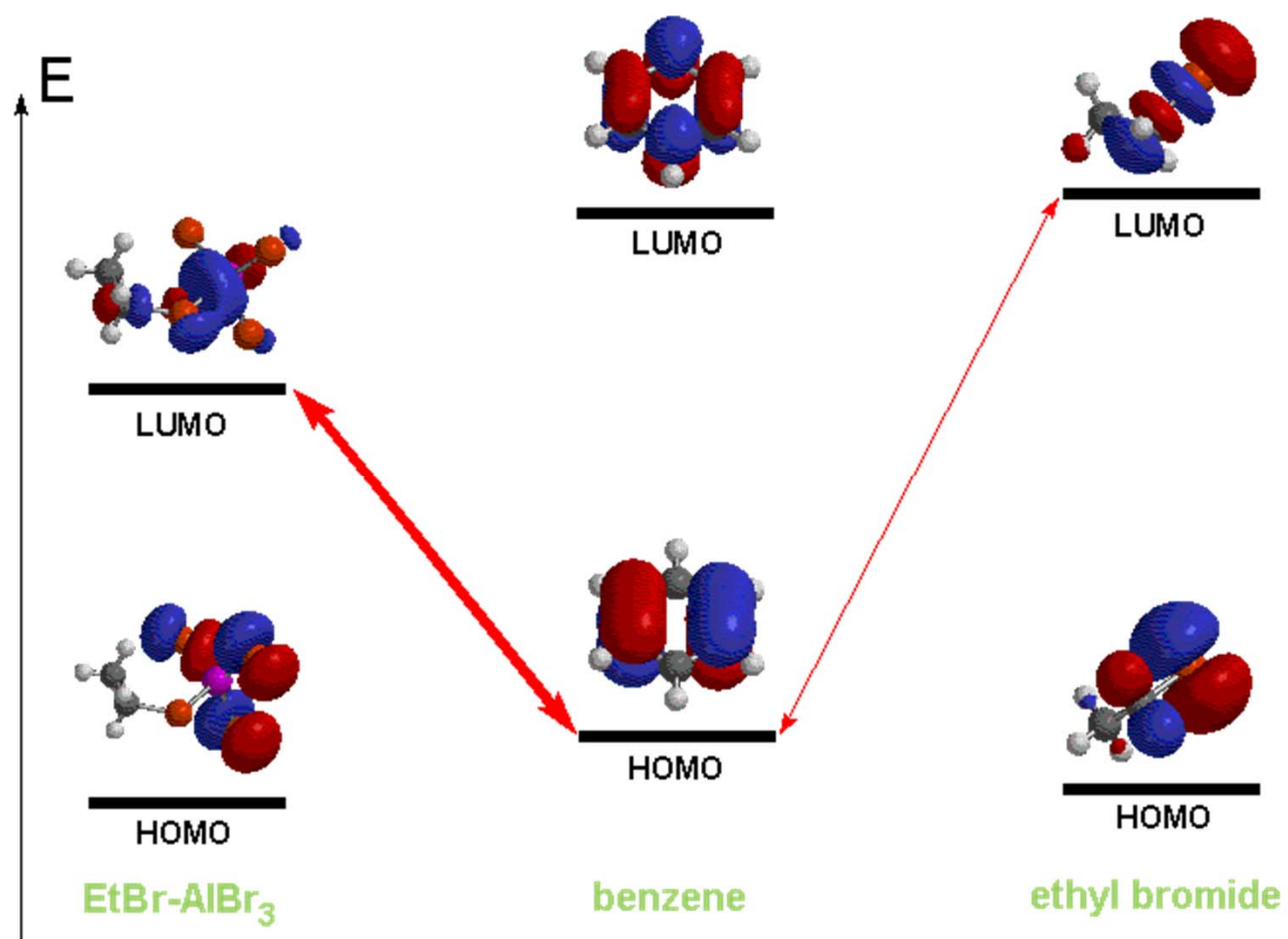
$$\psi_i = \sum_{\mu} c_{\mu i} \phi_{\mu}$$

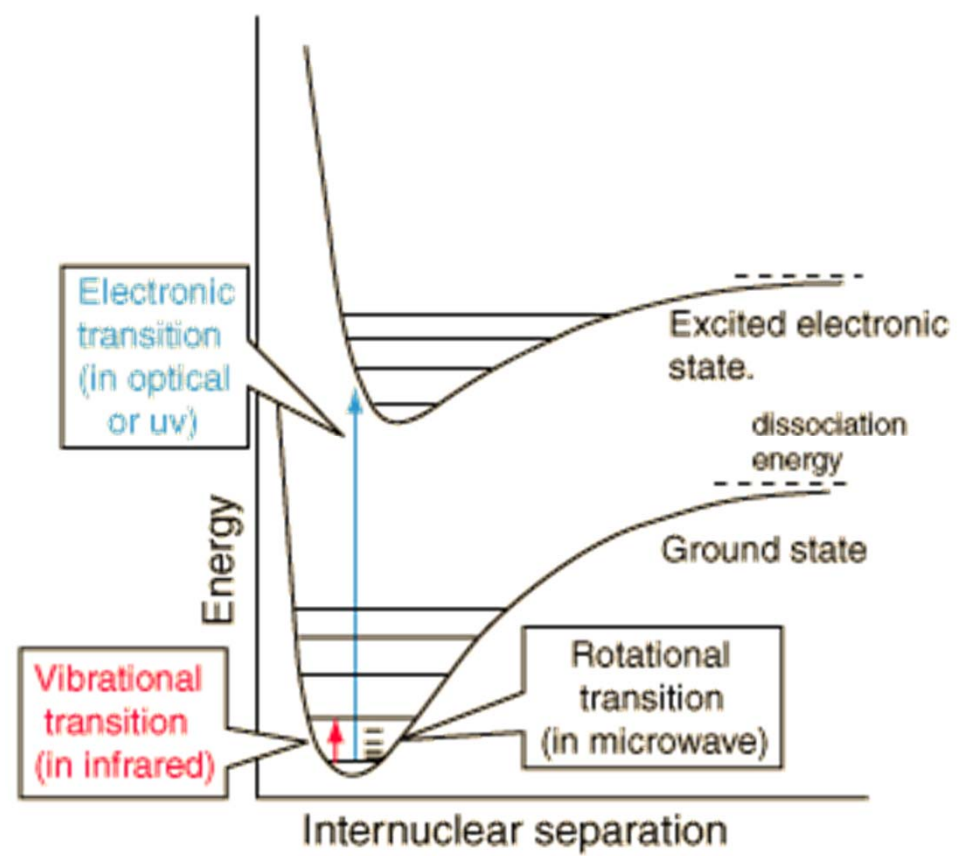
MO \nearrow \nwarrow coefficient of AO_{μ} in MO_i \nearrow AO

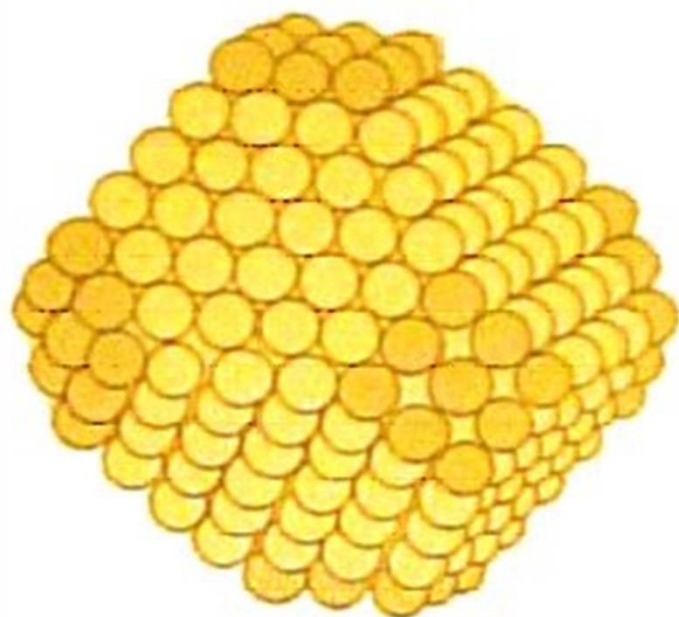


Oxygen









GOLD CUBOCTAHAL CLUSTER



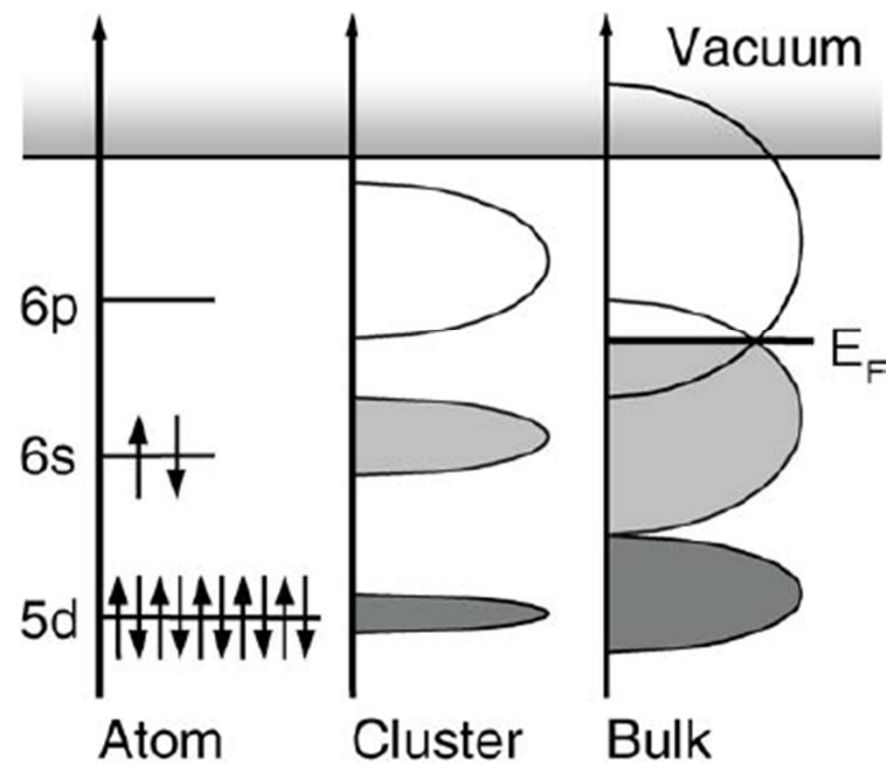


Figure 5 Energy diagram describing a generic Bloch-Wilson MIT in clusters (with specific reference to the energy levels of mercury). For sufficiently large clusters, the *s-p* band gap closes with increasing cluster size (shaded areas represent energy range with occupied electron levels). Overlap leads to a “continuous” DOS at E_F and to an Insulator to Metal transition.



Bloch wave

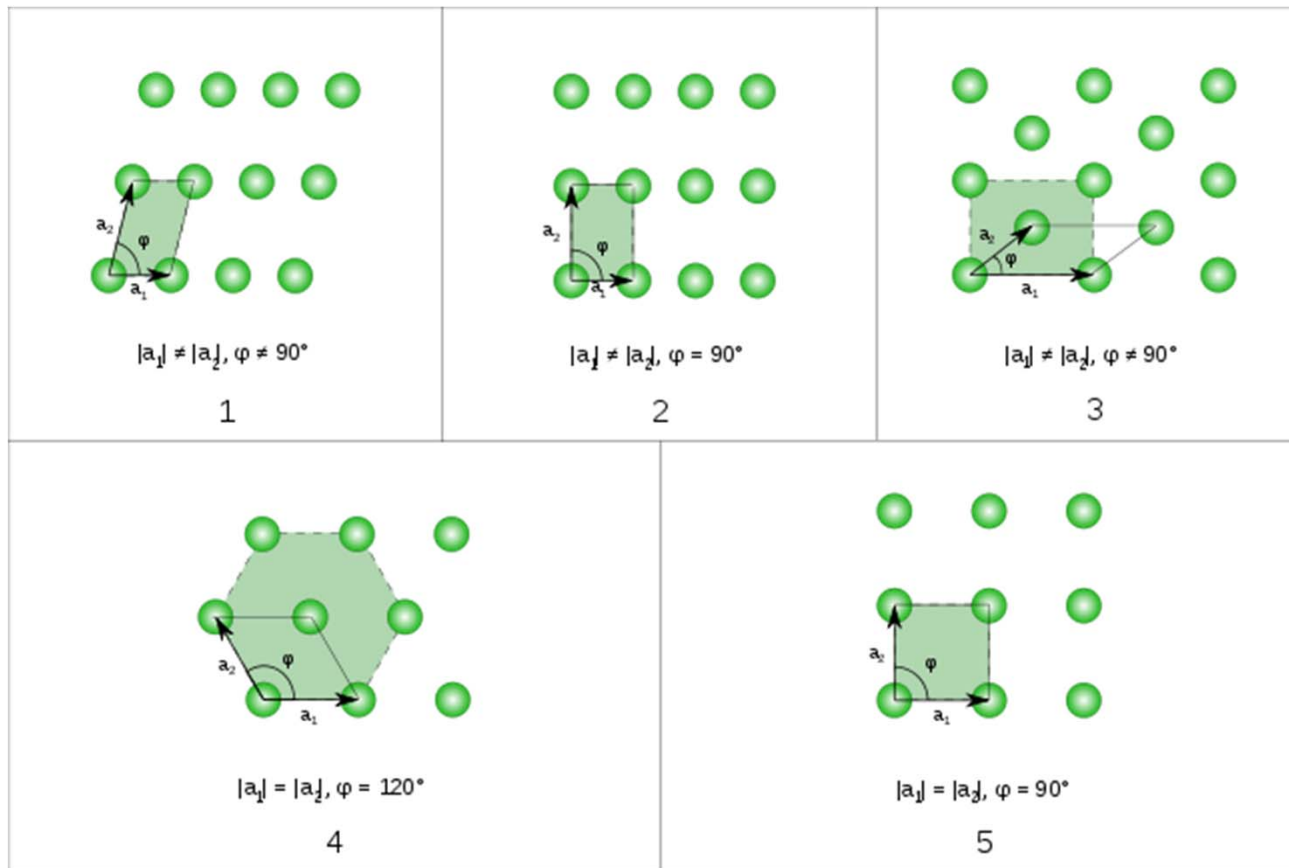
$$\psi_{n\mathbf{k}}(\mathbf{r}) = e^{i\mathbf{k}\cdot\mathbf{r}} u_{n\mathbf{k}}(\mathbf{r})$$

A **Bloch wave** or **Bloch state**, named after [Felix Bloch](#), is the [wavefunction](#) of a particle (usually, an [electron](#)) placed in a [periodic potential](#).

$$\epsilon_n(\mathbf{k}) = \epsilon_n(\mathbf{k} + \mathbf{K}),$$



The five fundamental two-dimensional Bravais lattices



Unit Cell

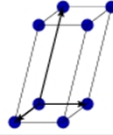
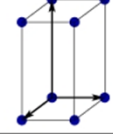
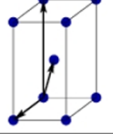
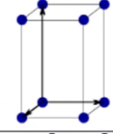
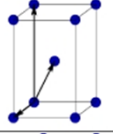
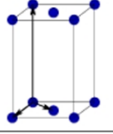
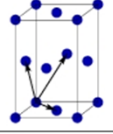
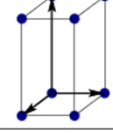
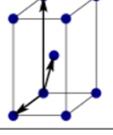
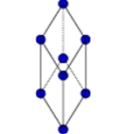
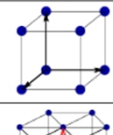
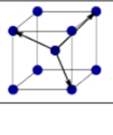
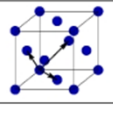
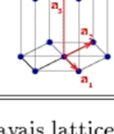
Bravais lattice	Parameters	Simple (P)	Volume centered (I)	Base centered (C)	Face centered (F)
Triclinic	$a_1 \neq a_2 \neq a_3$ $\alpha_{12} \neq \alpha_{23} \neq \alpha_{31}$				
Monoclinic	$a_1 \neq a_2 \neq a_3$ $\alpha_{23} = \alpha_{31} = 90^\circ$ $\alpha_{12} \neq 90^\circ$				
Orthorhombic	$a_1 \neq a_2 \neq a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90^\circ$				
Tetragonal	$a_1 = a_2 \neq a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90^\circ$				
Trigonal	$a_1 = a_2 = a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} < 120^\circ$				
Cubic	$a_1 = a_2 = a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90^\circ$				
Hexagonal	$a_1 = a_2 \neq a_3$ $\alpha_{12} = 120^\circ$ $\alpha_{23} = \alpha_{31} = 90^\circ$				

Table 1.1: Bravais lattices in three-dimensions.

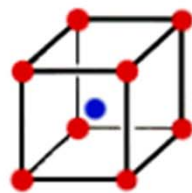




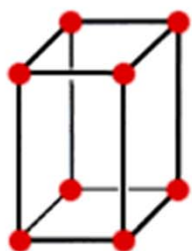
**Simple
cubic**



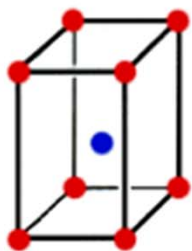
**Face-centered
cubic**



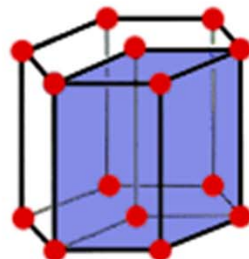
**Body-centered
cubic**



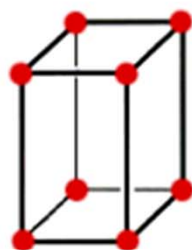
**Simple
tetragonal**



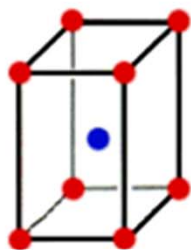
**Body-centered
tetragonal**



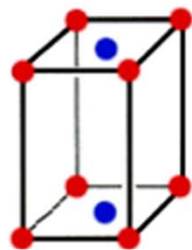
Hexagonal



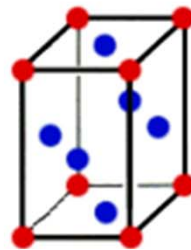
**Simple
orthorhombic**



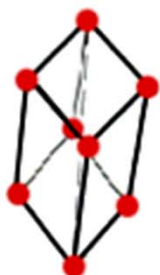
**Body-centered
orthorhombic**



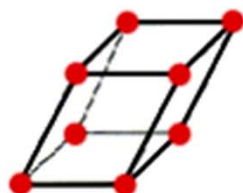
**Base-centered
orthorhombic**



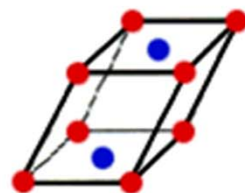
**Face-centered
orthorhombic**



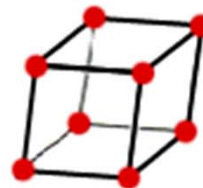
Rhombohedral



**Simple
Monoclinic**

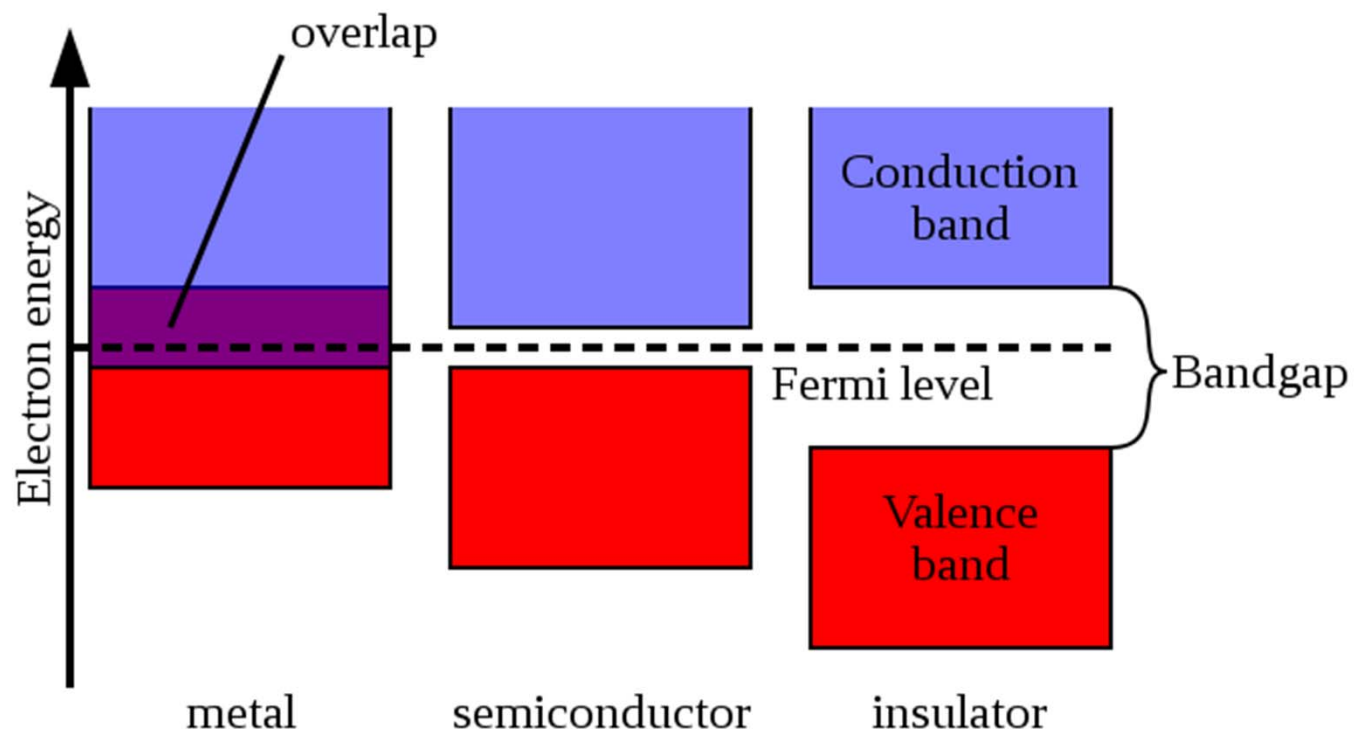


**Base-centered
monoclinic**

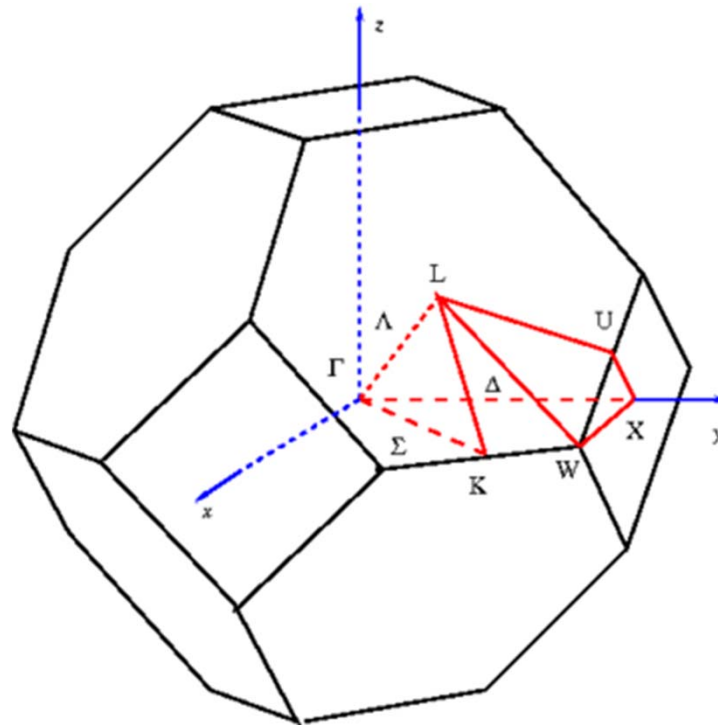


Triclinic

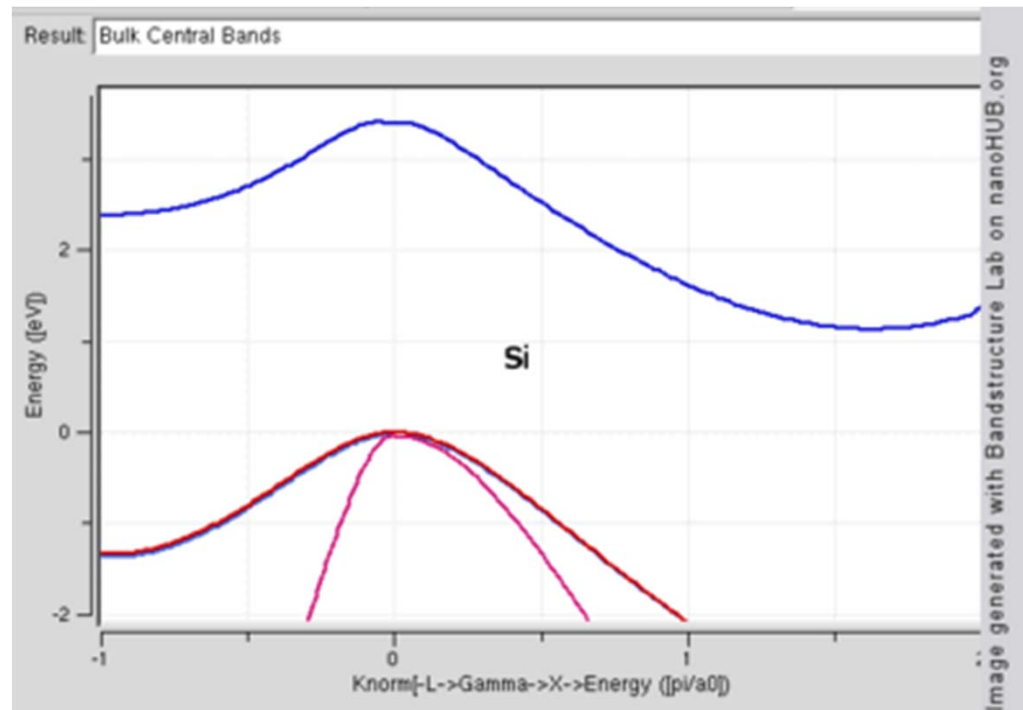




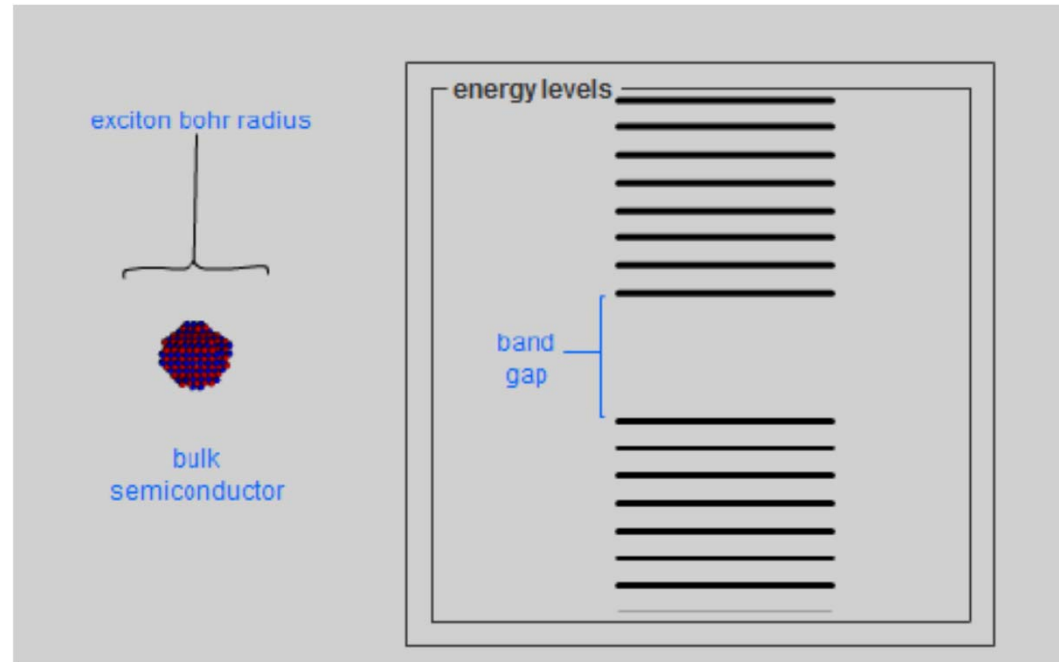
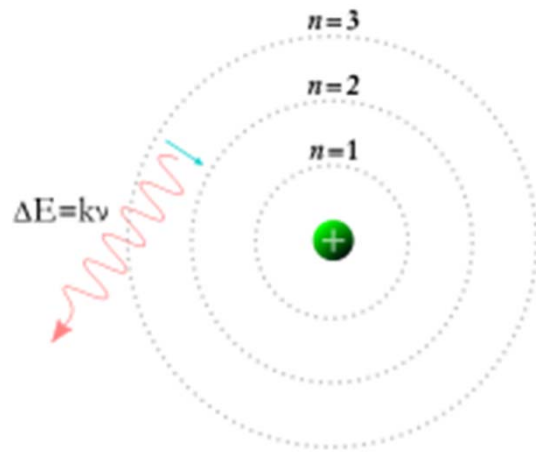
First Brillouin zone of FCC lattice showing symmetry labels

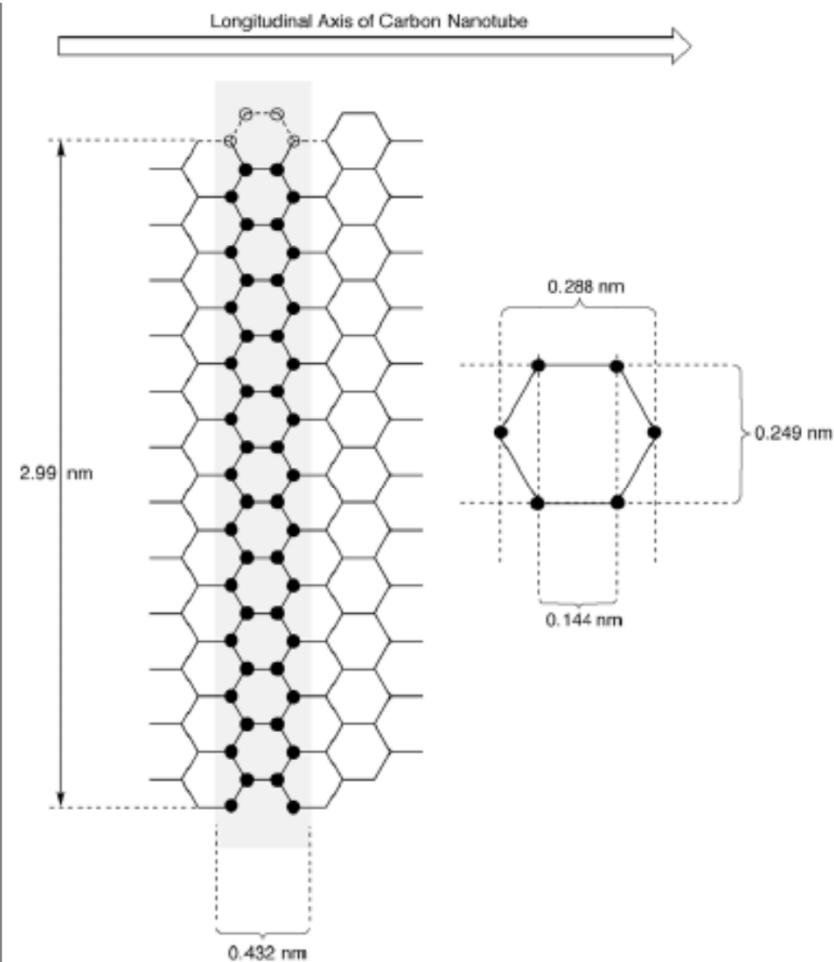


Band Structures



Bohr Exciton Radius





$$2a = 0.144 \text{ nm}$$

$$a = 0.072 \text{ nm}$$

$$(\text{Altitude})^2 = a^2 + 2a^2 = a^2 \sqrt{3}$$

$$\text{Minimal diameter} = 2 \cdot a \sqrt{3} = 2 \cdot (0.072) \text{ nm} \cdot \sqrt{3} = 0.249 \text{ nm}$$

$$\text{Circumference or Perimeter, } p = 12 \cdot 0.249 \text{ nm} = 2.988 \text{ nm}$$

$$p = \pi d; \text{ the } d = \frac{p}{\pi} = \frac{2.988 \text{ nm}}{\pi} = 0.951 \text{ nm}$$

$$m = \left(\frac{12.011 \text{ g}}{\text{mol}} \right) \left(\frac{1 \text{ mol}}{6.022 \times 10^{23} \text{ atoms}} \right) 48 \text{ atoms} = 9.573 \times 10^{-22} \text{ g}$$

$$V_{\text{unit cell}} = 0.432 \text{ nm} \cdot \pi r^2 = 0.432 \text{ nm} \cdot \pi \cdot \left(\frac{0.951 \text{ nm}}{2} \right)^2 = 0.307 \text{ nm}^3$$

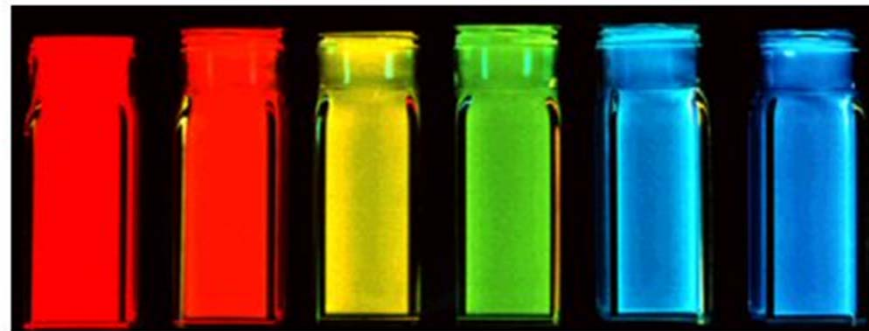
$$0.307 \text{ nm}^3 \left(\frac{\text{cm}}{10^7 \text{ nm}} \right)^3 = 3.07 \times 10^{-22} \text{ cm}^3$$

$$\rho = \frac{g}{\text{cm}^3} = \frac{9.573 \times 10^{-22} \text{ g}}{3.07 \times 10^{-22} \text{ cm}^3} = 3.12 \text{ g} \cdot \text{cm}^3$$

$$S_{\text{Unit-cell}} = \frac{p \cdot W}{m} = \frac{2.99 \text{ nm} \cdot 0.432 \text{ nm}}{9.573 \times 10^{-22} \text{ g}} \left(\frac{\text{m}}{10^9 \text{ nm}} \right)^2 = 1.35 \times 10^3 \text{ m}^2 \cdot \text{g}^{-1}$$



CdSe



6.5 nm



5.5 nm



4.0 nm



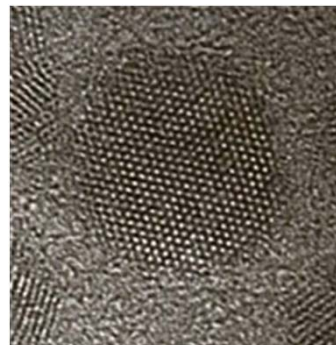
3.0 nm



2.5 nm



2.0 nm



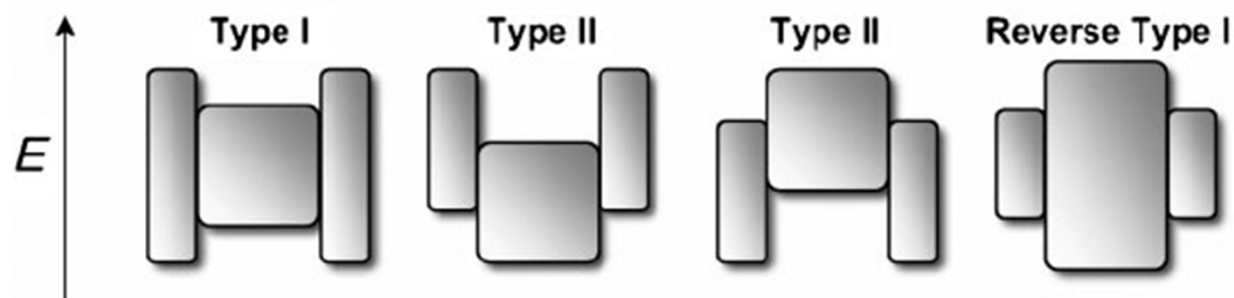
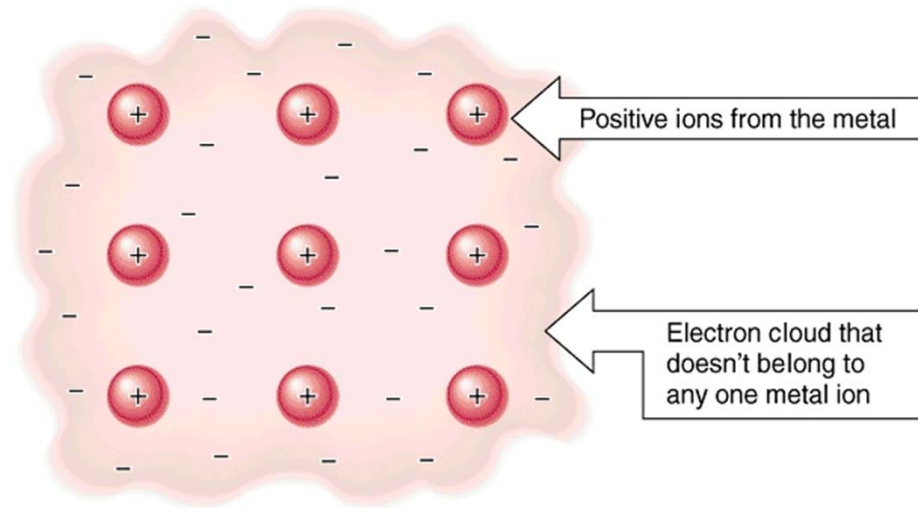
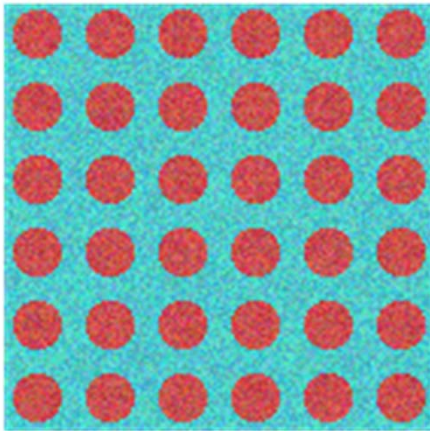


Figure 1. Schematic representation of the energy-level alignment in different core/shell systems realized with semiconductor NCs to date. The upper and lower edges of the rectangles correspond to the positions of the conduction- and valence-band edge of the core (center) and shell materials, respectively.



Electron Sea



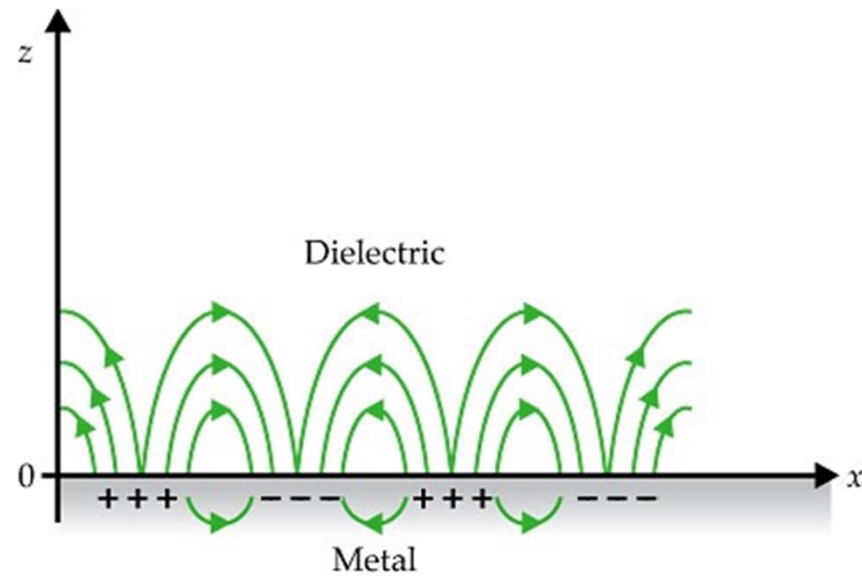
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$$m \frac{d^2 \delta x}{dt^2} = e E_x = -m \omega_p^2 \delta x,$$

$$\omega_p^2 = \frac{n e^2}{\epsilon_0 m},$$



Surface Plasmon



$$\epsilon_m = 1 - \frac{\omega_p^2}{\omega^2}$$



TiO₂

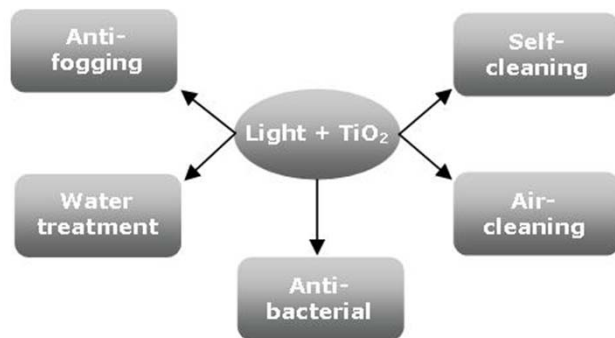
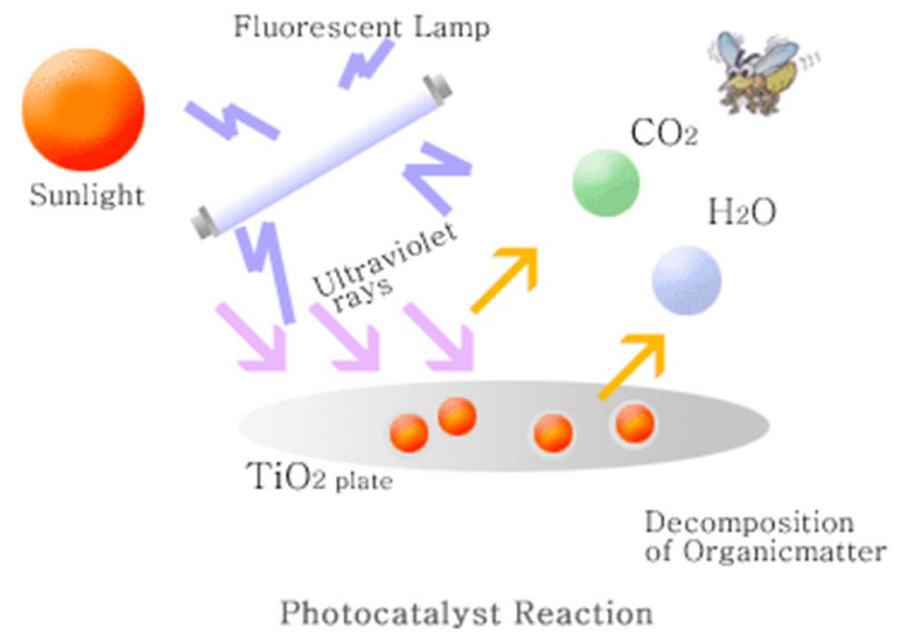
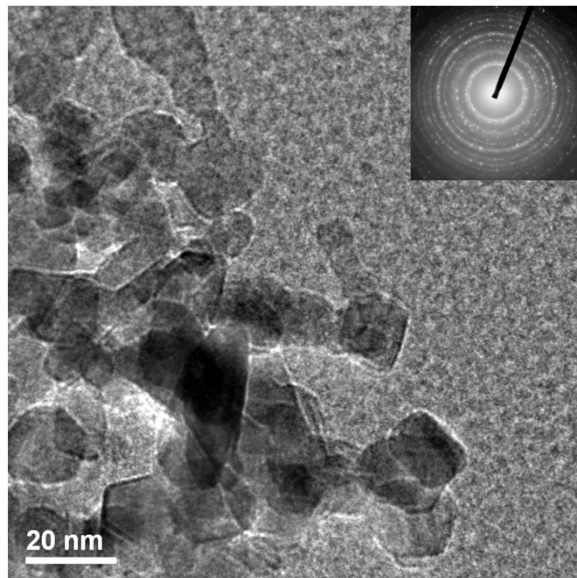
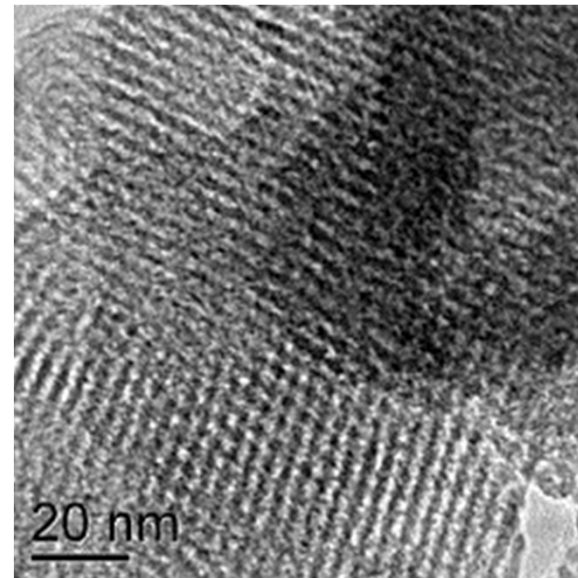
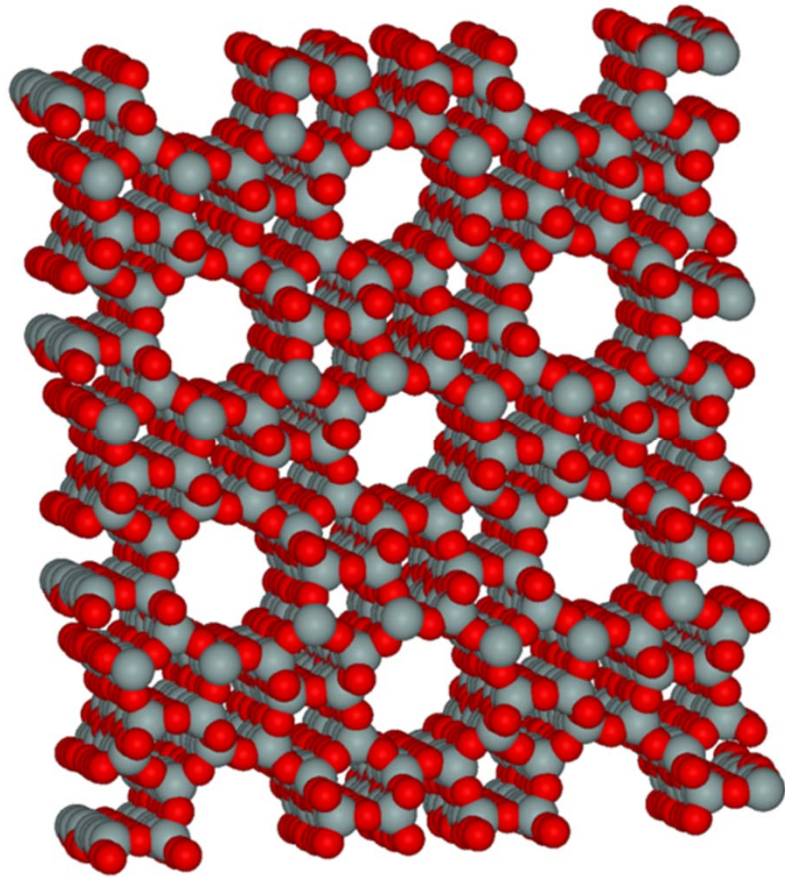


Figure 1. Major areas of activity in titanium dioxide photocatalysis



Zeolite



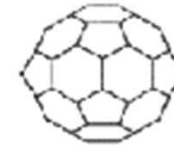
Carbon



SWNT



Poly-C₆₀



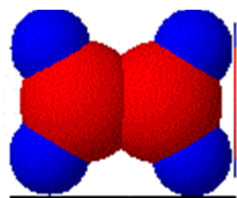
C₆₀



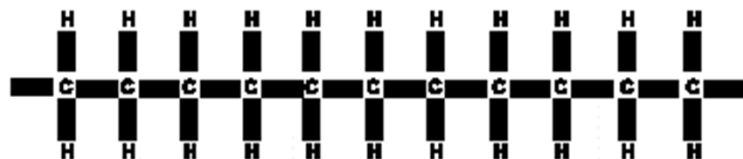
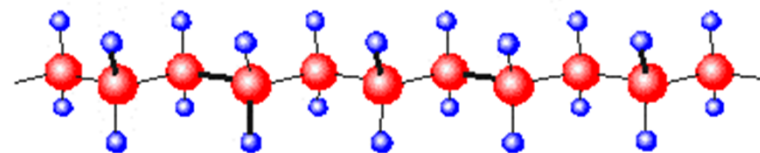
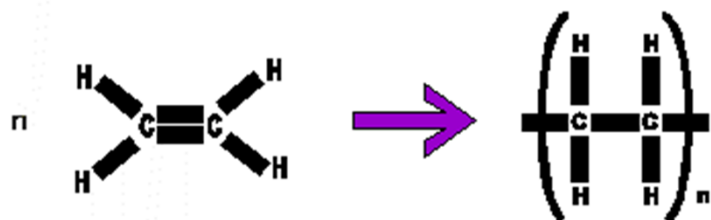
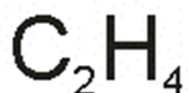
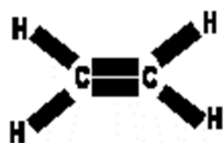
Nanodiamond
~ 2-10 nm



Polymer

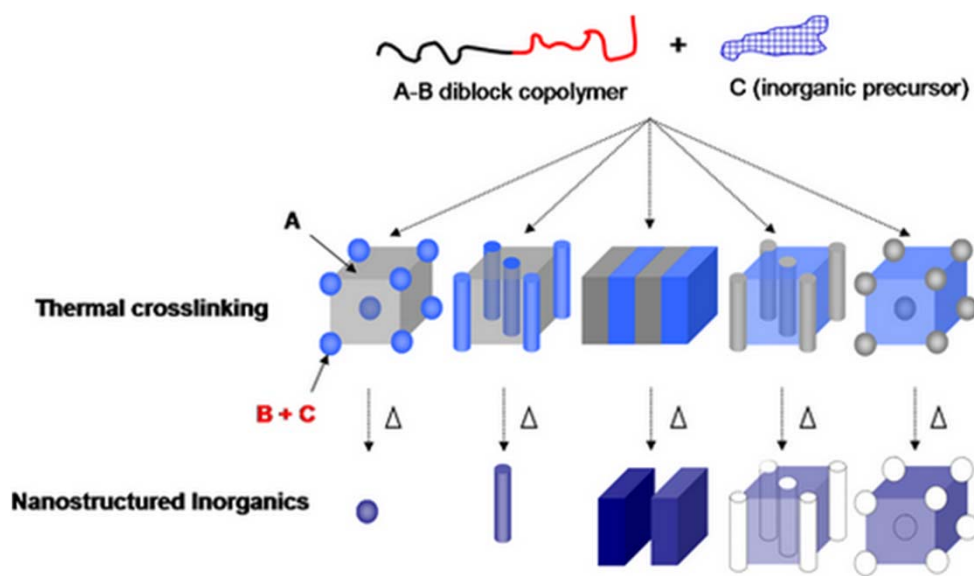


a monomer ethene

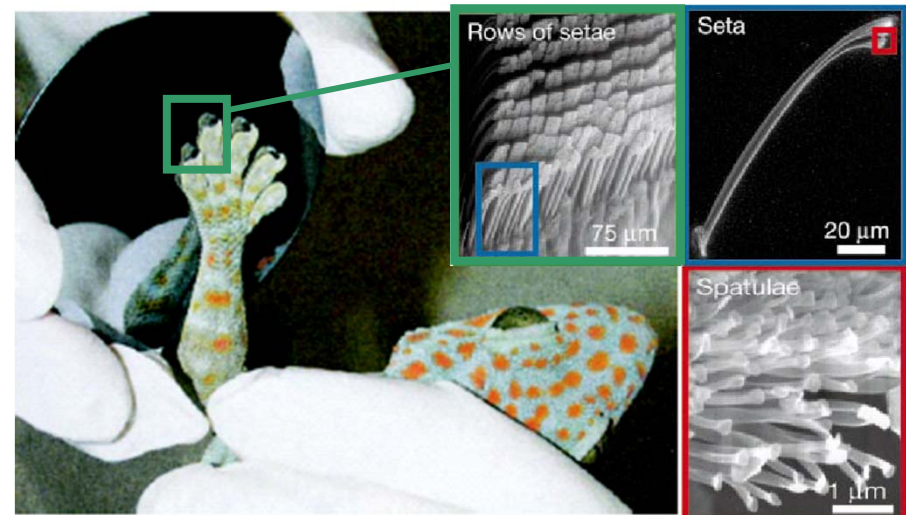
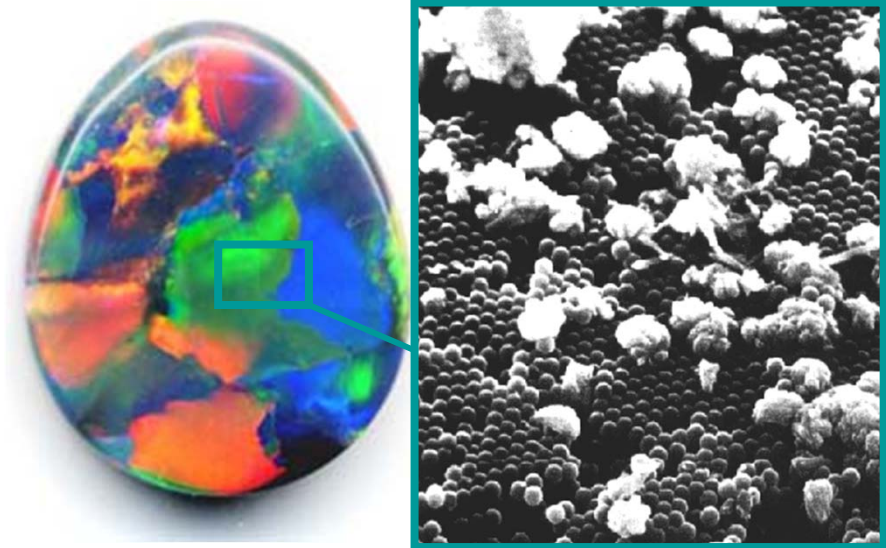
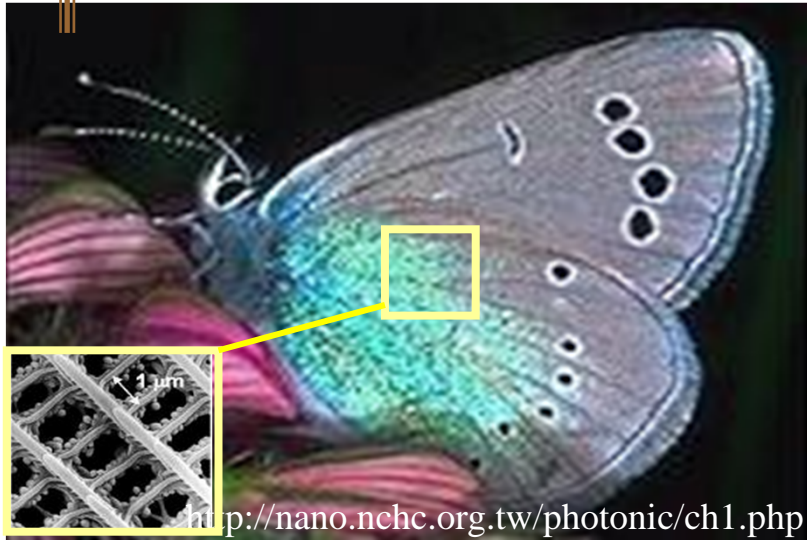


a polymer

poly(ethene)



Nature Materials



Surface Energy

One face surface energy: γ

27 cube: $27 \times 6 \gamma$

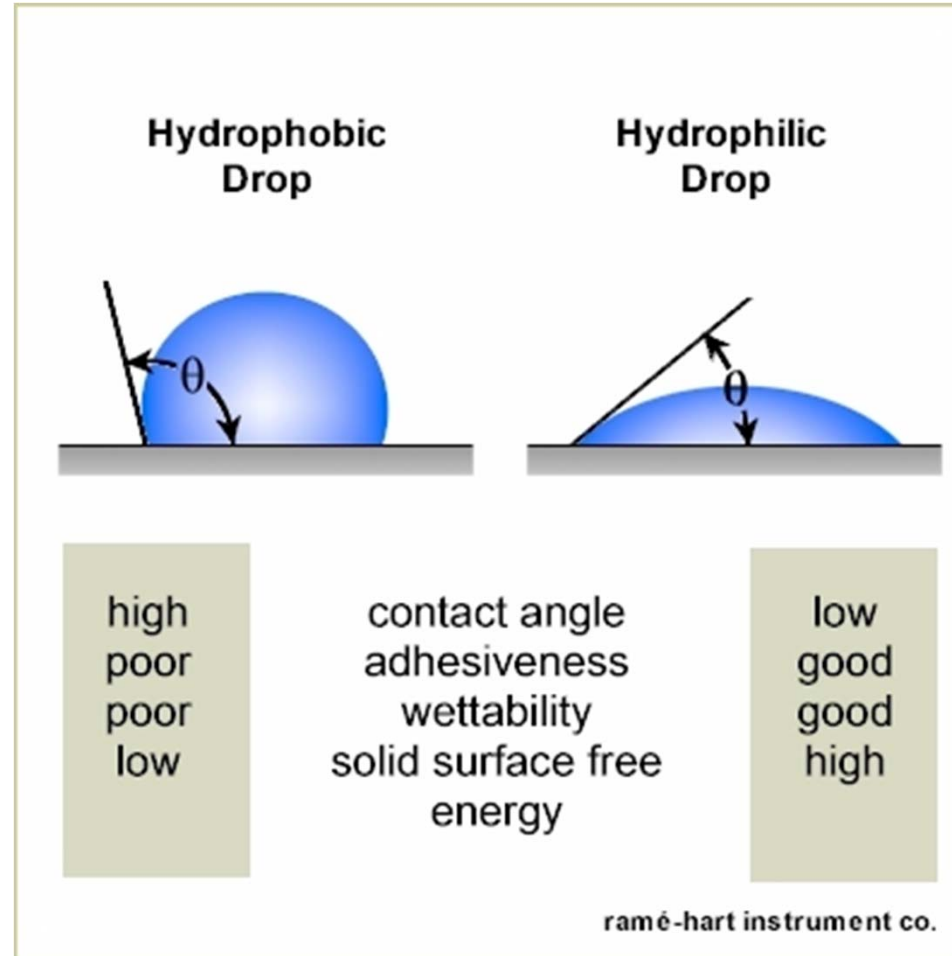
3 x 9 cube line: 114γ

3 x (3x3) square: 90γ

3 x 3 x 3 cube: 54γ

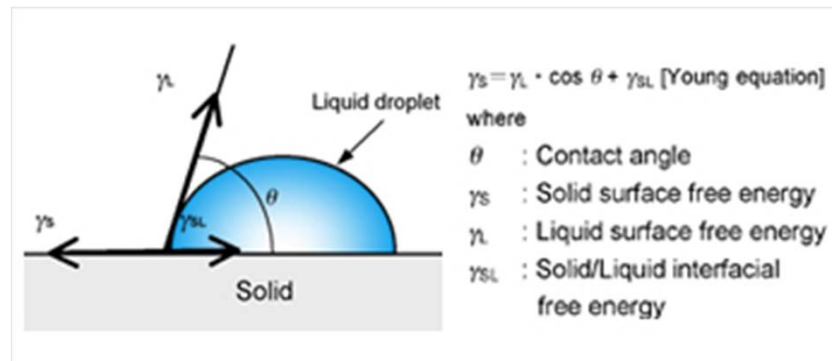


Contact Angle



Young's Equation

$$\gamma_{SL} + \gamma_{LV} \cos \theta_c = \gamma_{SV}$$

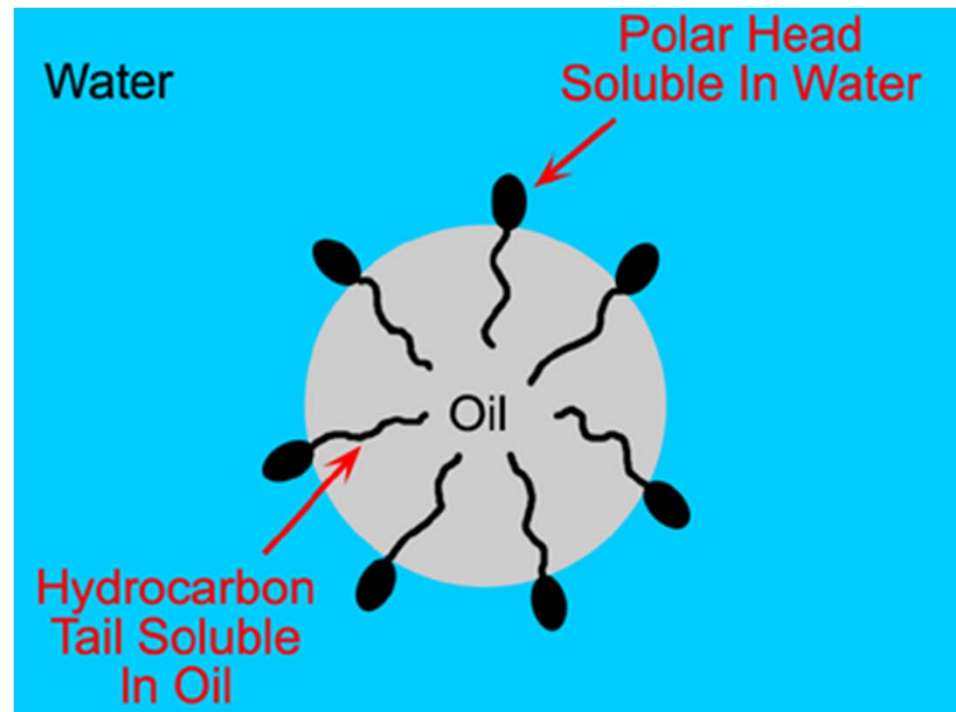


Surface Energy Minimization

- Surfactants
- DLVO
- Polymeric
- Nucleation
- Ostwald Ripening
- Sintering
- Restructure



Surfactant



DLVO Theory

$$V_T = V_A + V_R + V_S$$

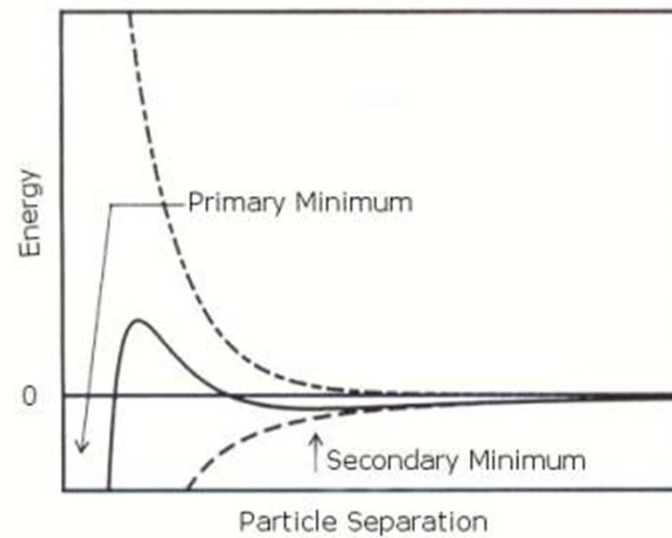
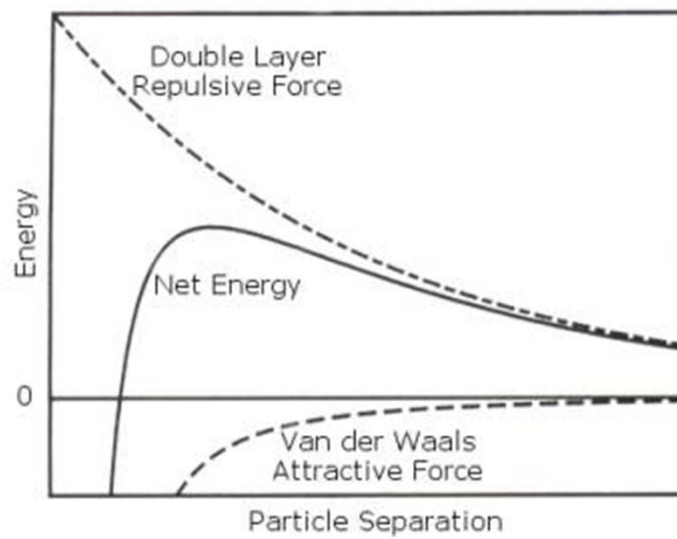
$$V_A = -A/(12 \pi D^2)$$

A is the Hamaker constant and D is the particle separation

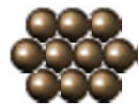
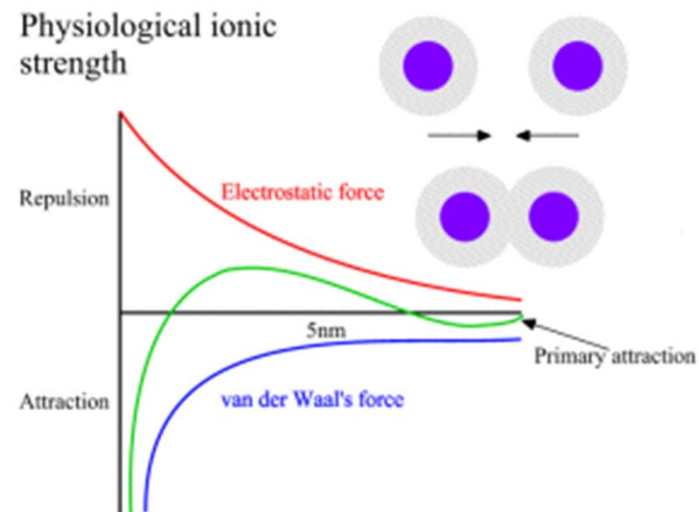
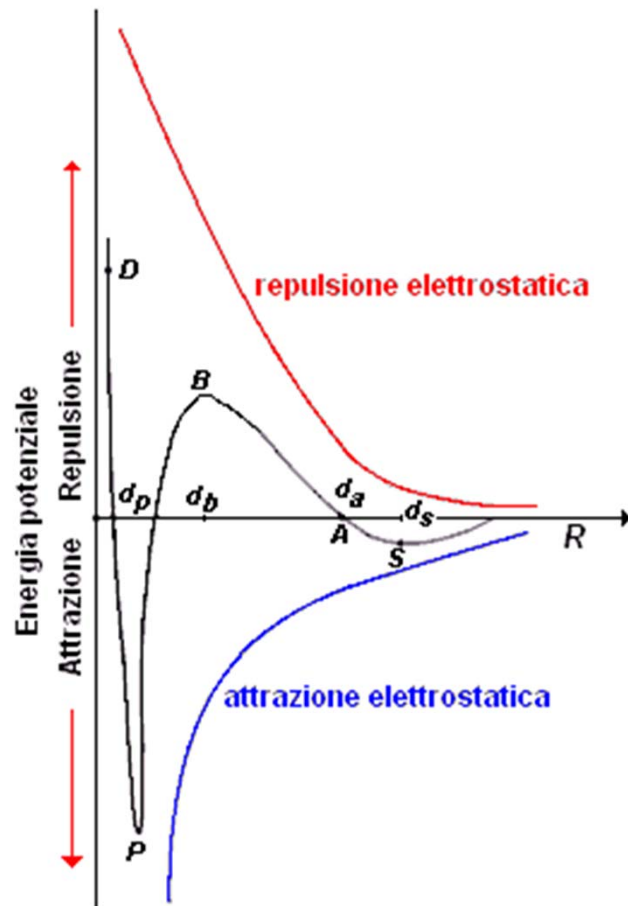
$$V_R = 2 \pi \epsilon a \xi^2 \exp(-\kappa D)$$

a is the particle radius, π is the solvent permeability,
 κ is a function of the ionic composition and ξ is the zeta potential

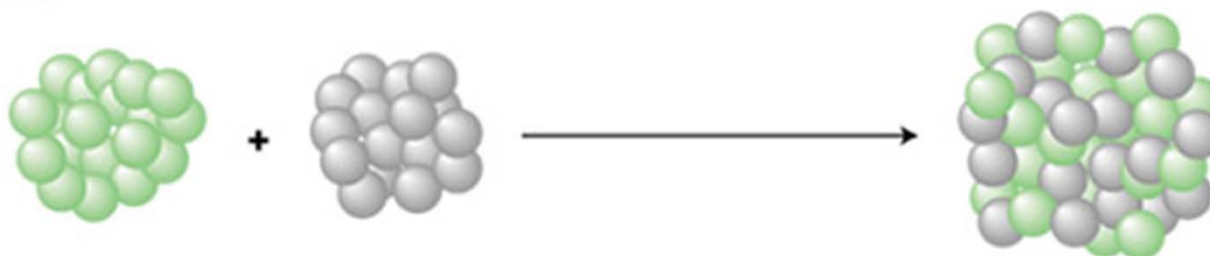




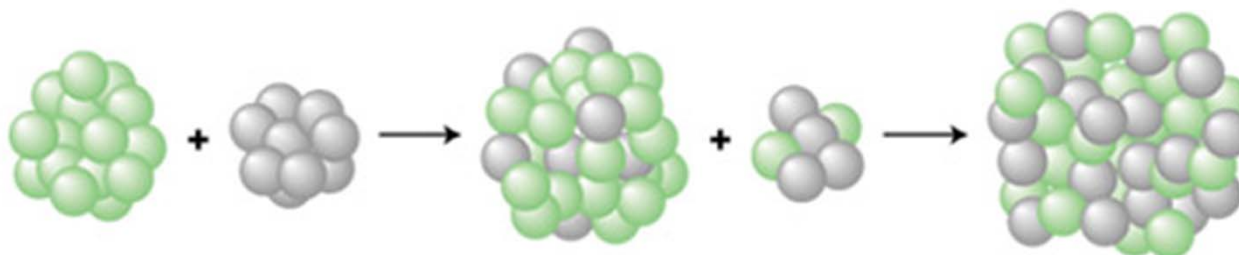
DLVO Theory



a Coalescence



b Ostwald ripening



Two main mechanisms are shown here: **a**, coalescence sintering, and **b**, Ostwald ripening sintering. Coalescence sintering occurs when two clusters touch or collide and merge to form one bigger cluster. In contrast, Ostwald ripening sintering occurs by evaporation of atoms from one cluster, which then transfer to another. This is a dynamic process — both clusters exchange atoms, but the rate of loss from the smaller cluster is higher, because of the lower average coordination of atoms at the surface and their relative ease of removal. Thus big clusters get bigger at the expense of smaller clusters, which shrink and eventually disappear. The latter process is the usual form of sintering for metal clusters on a supported surface that are well spaced apart, although coalescence can occur for a high density of clusters. In general, the presence of the surface results in SMORS (surface-mediated Ostwald ripening sintering) in which material is transferred from one cluster to another by diffusion across the surface, and not through the gas phase.

